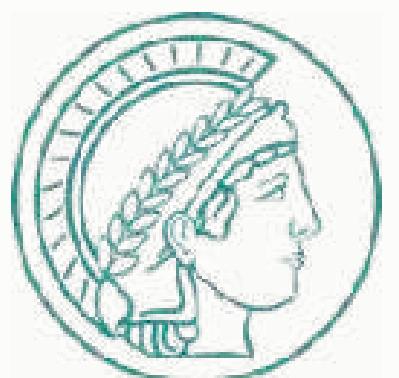


Challenges of data driven modelling in cardiac dynamics

Ulrich Parlitz

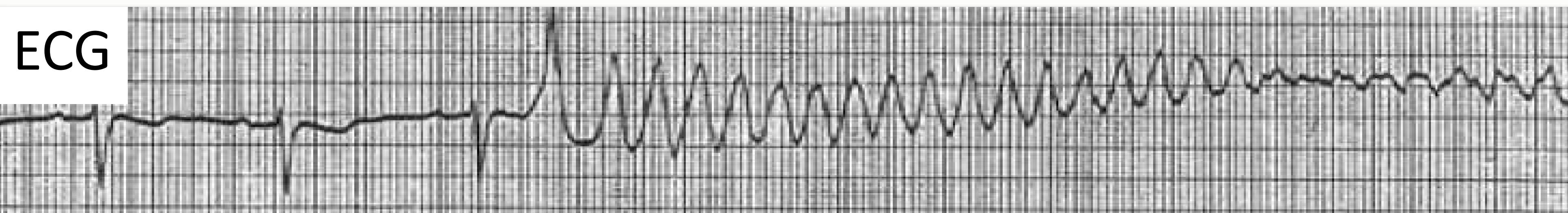
Research Group Biomedical Physics
Max Planck Institute for Dynamics and Self-Organization
Göttingen, Germany



Institute for the Dynamics of Complex Systems
University of Göttingen, Germany

Transitions to Cardiac Arrhythmias

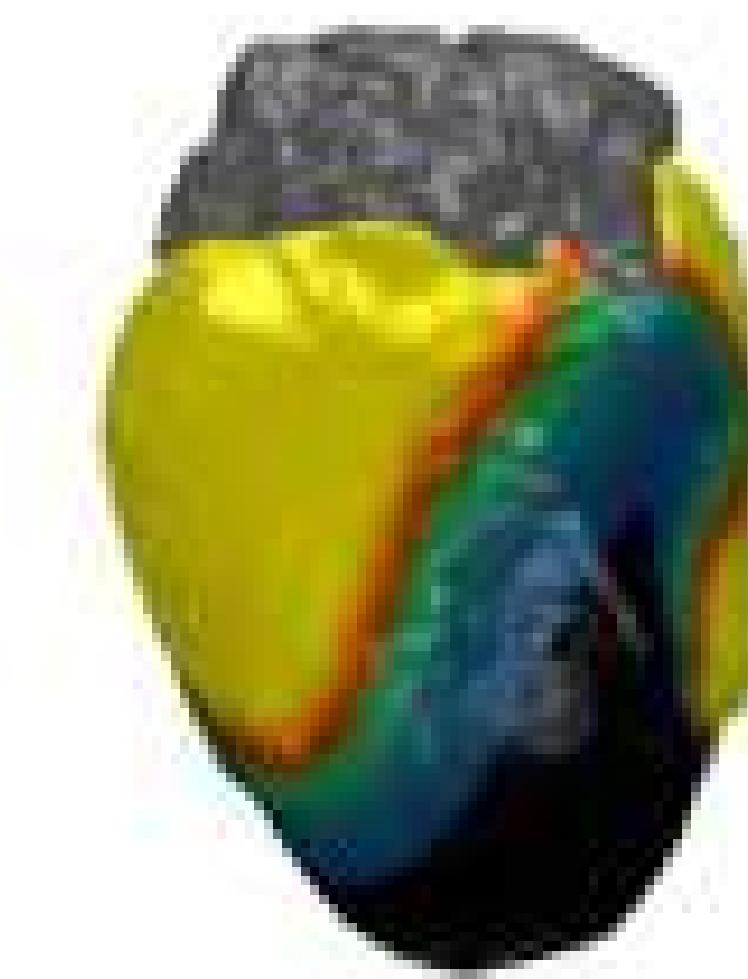
Normal Rhythm → Tachycardia → Fibrillation



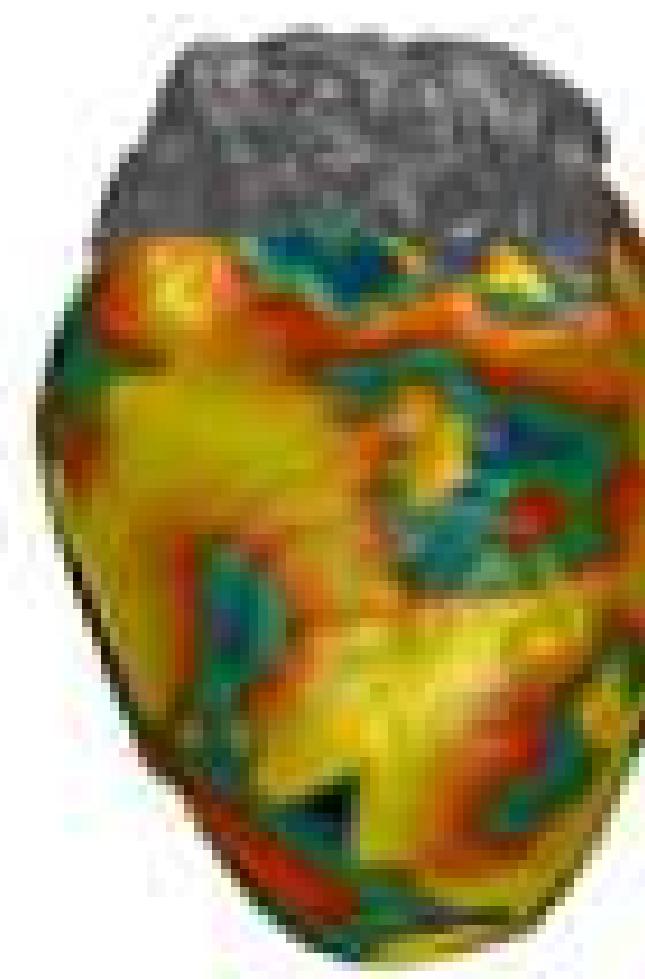
electrical excitation waves



plane waves



spiral waves



chaos

simulations: P. Bittihn

Challenges for diagnosis and therapy

- develop tools for observing the dynamics of arrhythmias (e.g., novel measurement modalities and advanced methods for data analysis)
- understand conditions for the onset of cardiac arrhythmias and characterise their dynamical features
- devise minimal invasive methods for terminating (lethal) states of arrhythmias like ventricular fibrillation (avoiding strong shocks with high local currents)

Potential contributions from dynamical systems theory
and data driven modelling?

Characterization of Cardiac Arrhythmias

The heart: A Network of Cardiomyocytes

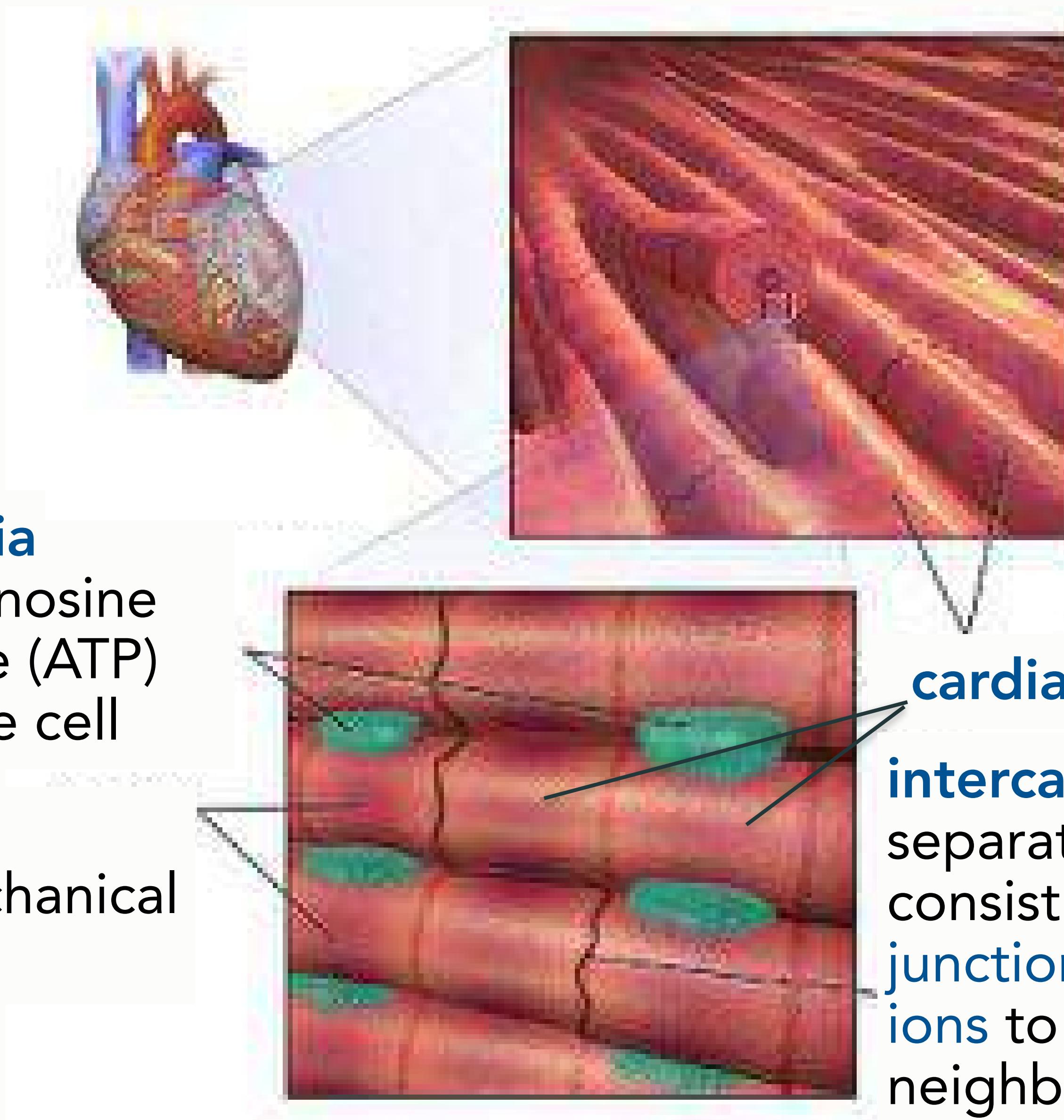
cardiac muscle

mitochondria

provide adenosine triphosphate (ATP) supply of the cell

myofibrils

provide mechanical contraction



cardiac muscle fibers

BruceBlaus - Own work, CC BY-SA 4.0,
<https://commons.wikimedia.org/w/index.php?curid=44969447>

Ventricular Cell

~ $10\mu\text{m} \times 100\mu\text{m}$

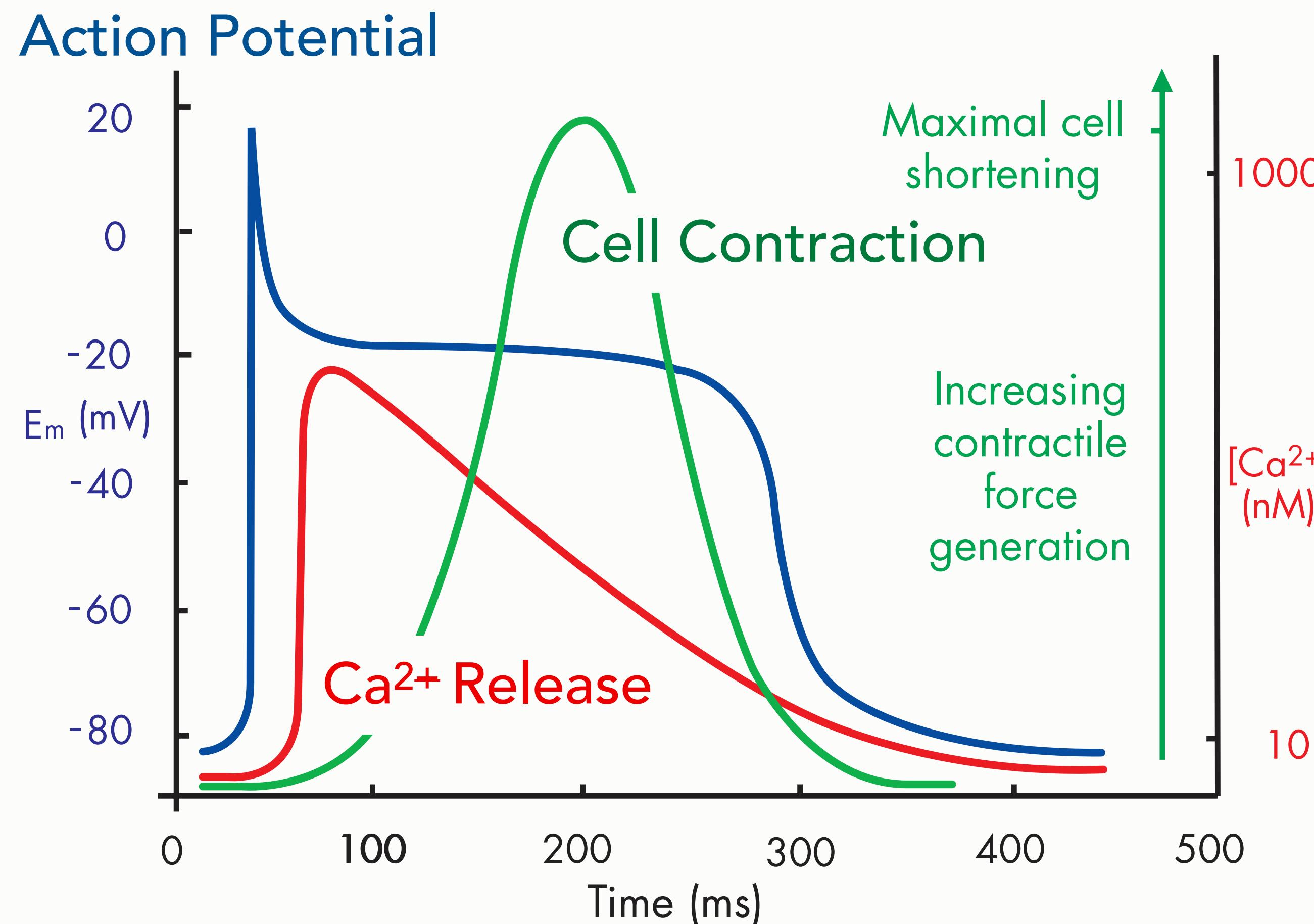


cardiac muscle cells

intercalated discs separate cells and consist of **gap junctions** that allow **ions** to propagate to neighbouring cell

© Kornreich & Fenton

Excitation-Contraction Coupling



electrical excitation

mechanical contraction

Mechanical perturbation
induces electrical stimulation via
stretch activated ion channels.

→ Commotio Cordis

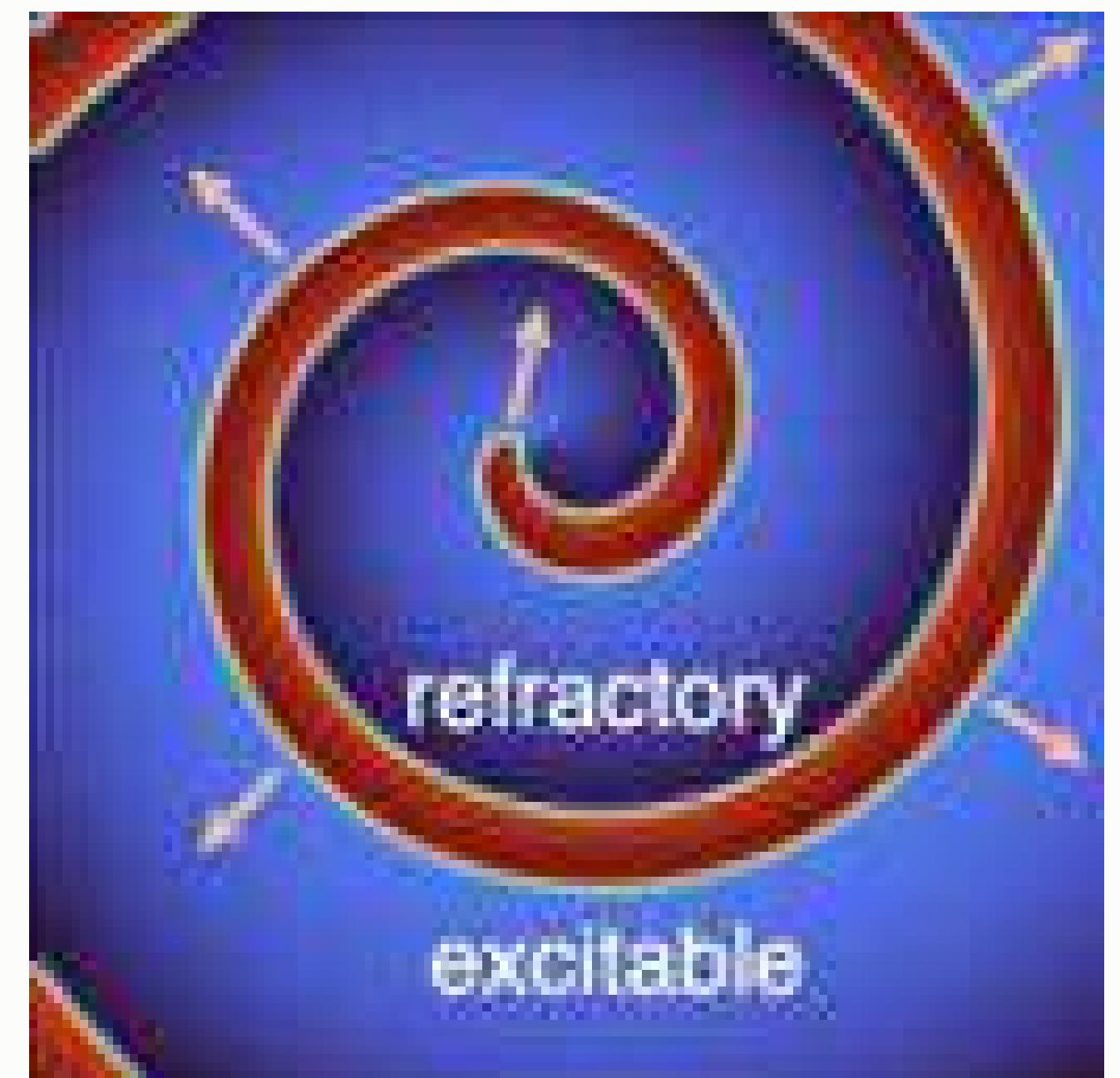
from: M. Scoote et al., Heart 89, 371–376 (2003)

Excitable Media

- An **excitable medium**
- is a **spatially extended nonlinear dynamical system**
- which has the capacity to **propagate excitation waves**,
- and which **cannot support** the passing of another wave until some time has passed (**refractory period/phase**)
→ **refractory region/zone**

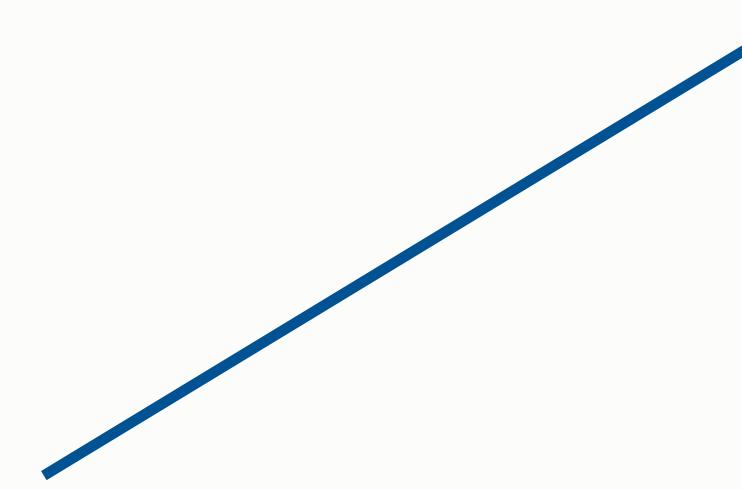
The existence of a **refractory region** means that an **excitation wave cannot propagate in any direction** but only to the excitable region of the medium.

As a result, **rotating waves**, also called **spiral waves** may occur.



The spatiotemporal Fitzhugh-Nagumo model

$$\begin{aligned}\dot{u} &= au(u - b)(1 - u) - w + d\Delta u \\ \dot{w} &= \varepsilon(u - w)\end{aligned}$$



spatial coupling via diffusion term

spatial domain with no-flux boundary conditions

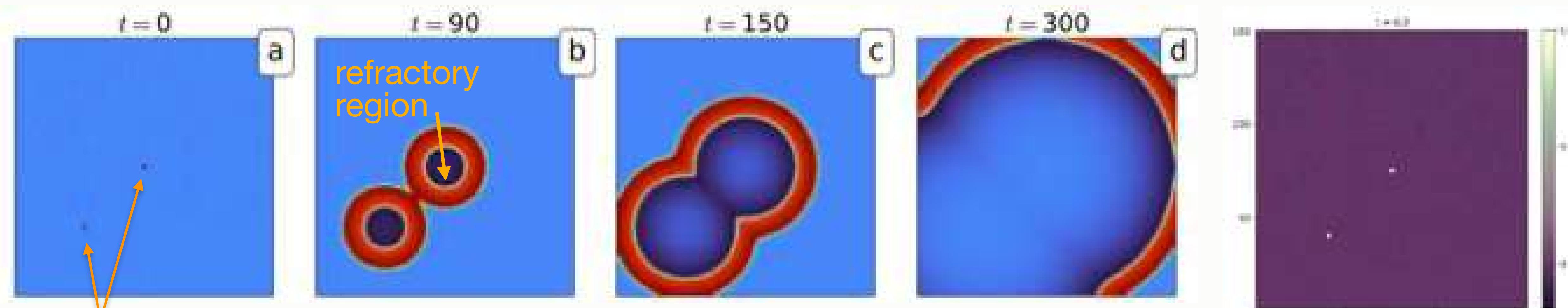
Depending on initial conditions and specific perturbations plane waves, concentric waves or spiral waves can be generated.

fundamental model describing
an excitable medium

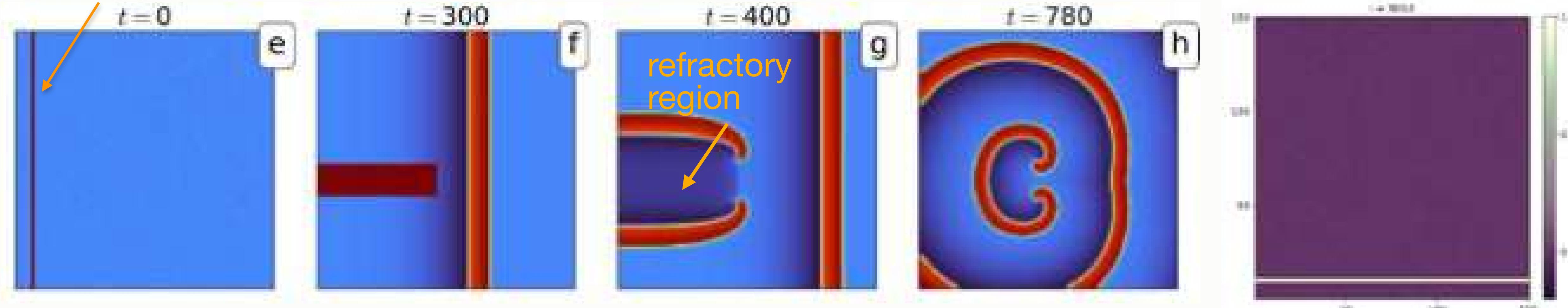
Excitable Media

Fitzhugh-Nagumo model

$$a = 3, b = 0.2, \varepsilon = 0.01, d = 1$$



initial local excitation



Mathematical Models of Cardiac Dynamics

continuum models averaging electrical behaviour of many cells

detailed ionic models: e.g., Luo-Rudy-II (15), Majahan (27), Bondarenko (44), ...

membrane
voltage

$$\frac{\partial V_m}{\partial t} = \nabla \cdot \underline{\mathbf{D}} \nabla V_m - I_{\text{ion}}(V_m, \mathbf{h})/C_m$$

ionic currents

$$\frac{\partial \mathbf{h}}{\partial t} = \mathbf{H}(V_m, \mathbf{h})$$

local cell dynamics (15-30 variables, 150 - 300 parameters!)

$$I_{\text{ion}}(V_m, \mathbf{h}) = \sum_x I_x(V_m, \mathbf{h}) + I_{\text{injection}}$$

generic qualitative models: e.g., Fenton-Karma (3), Beeler-Reuter (8), ...

simple qualitative models: e.g., Barkley (2), FitzHugh-Nagumo (2), Aliev-Panfilov (2), ...

see Scholarpedia article by F. Fenton and E. Cherry discussing 45 models of cardiac cells

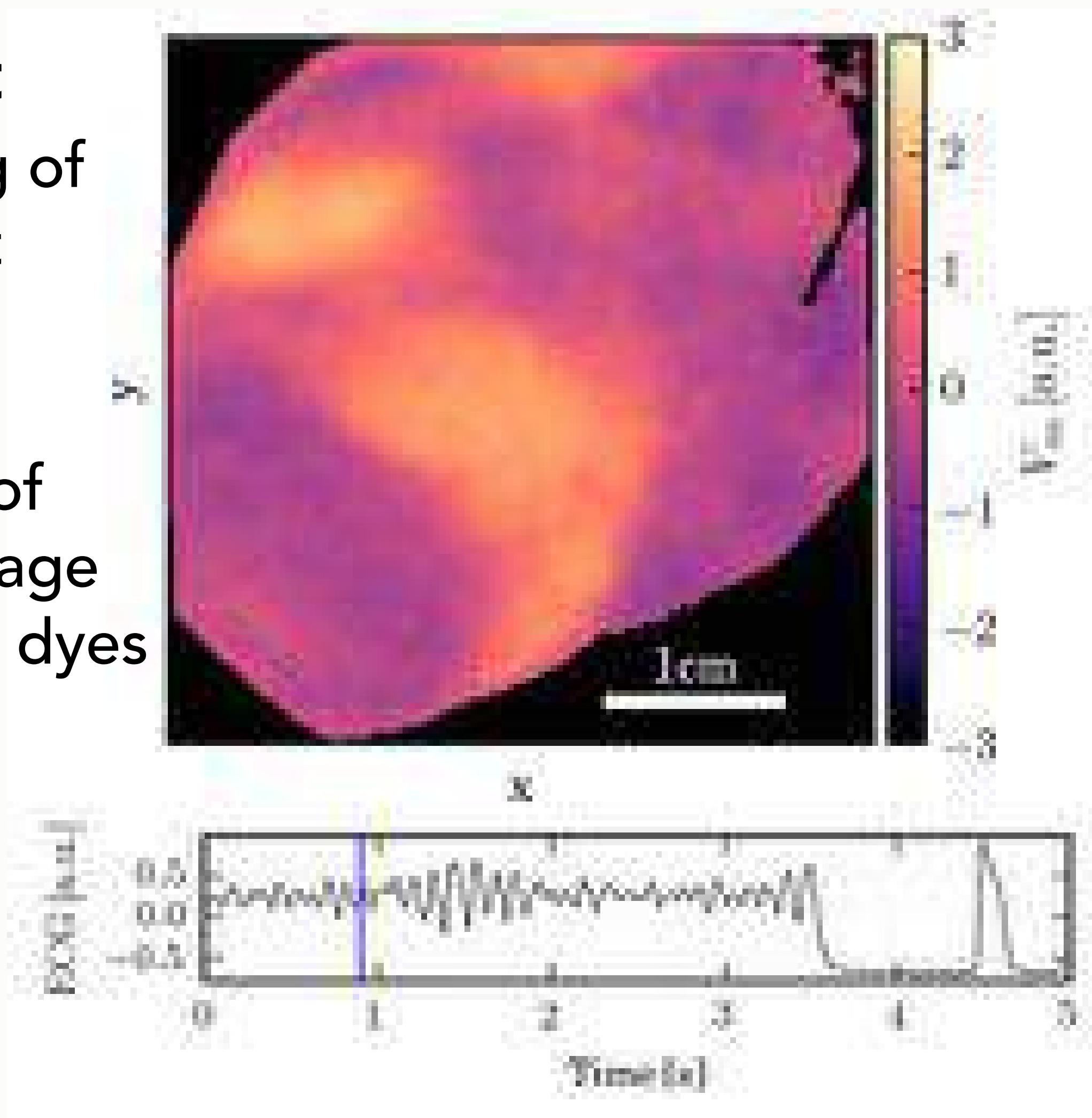
Transient Chaos

Transient Scroll Wave Dynamics during Ventricular Fibrillation

Experiment

Optical mapping of
a rabbit heart

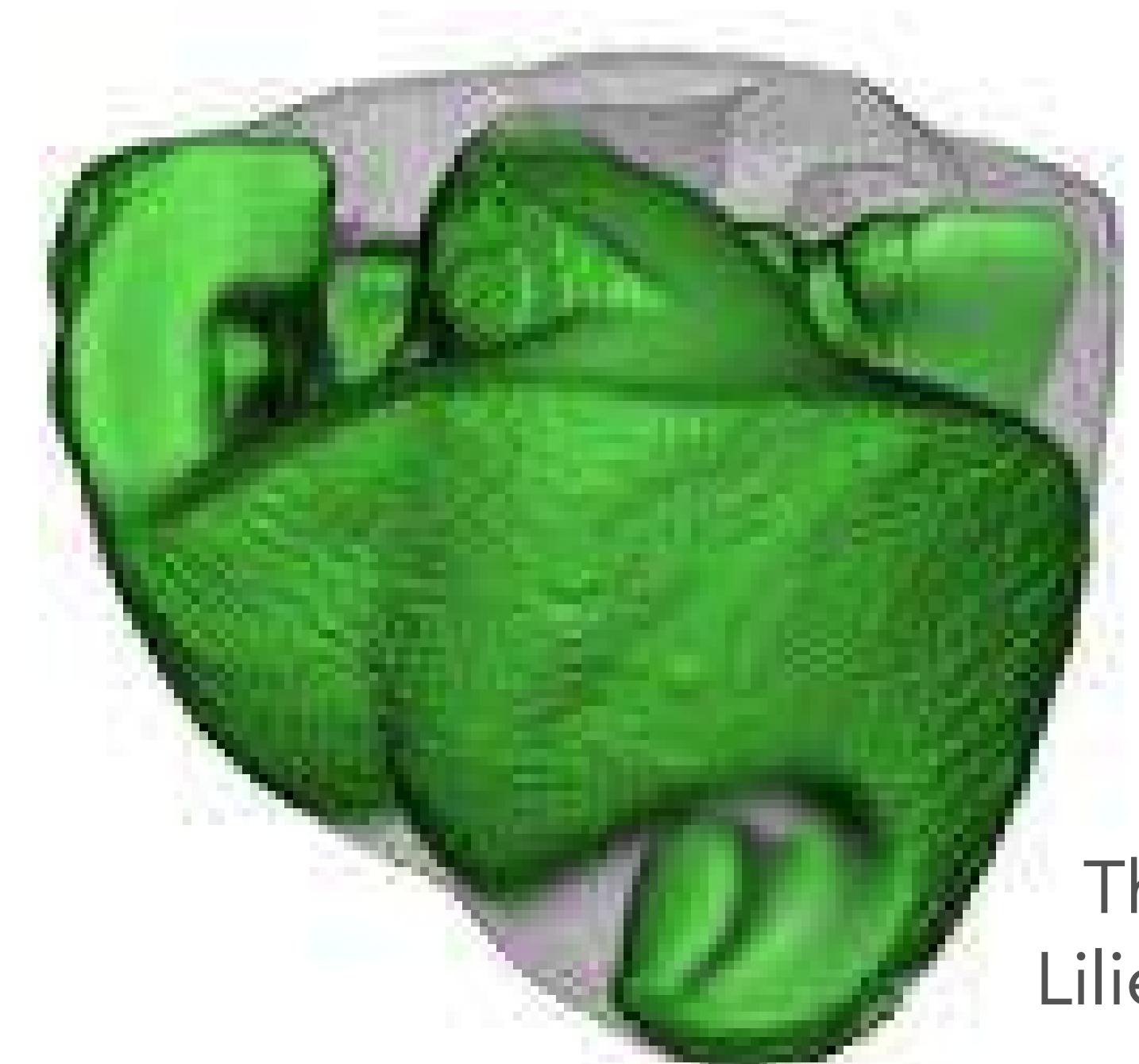
Visualisation of
membrane voltage
using fluorescent dyes



Sebastian Berg
Daniel Hornung
Marion Kunze

Simulation

in a rabbit heart geometry



Thomas
Lilienkamp

Transient events of fibrillation have also
been observed with human patients.

$$T_{\text{transient}} < T_{\text{survival}}$$

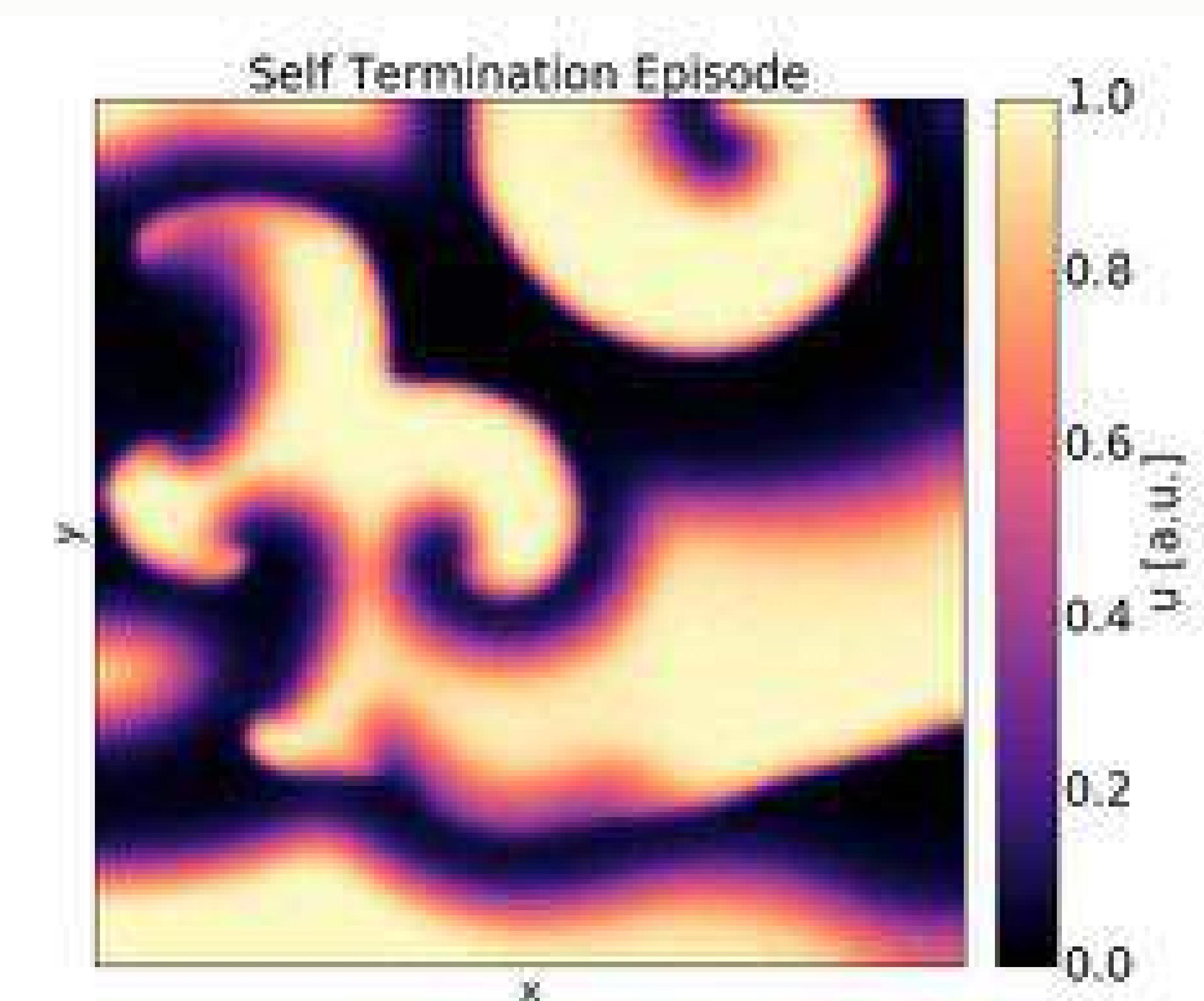
Transient Chaos

Transient chaos in the Fenton-Karma model

$$\begin{aligned}\frac{\partial u}{\partial t} &= \nabla \cdot \underline{\mathbf{D}} \nabla u - I_{Ion}(u, \mathbf{h})/C_m \\ \frac{\partial \mathbf{h}}{\partial t} &= \mathbf{g}(u, \mathbf{h})\end{aligned}$$

gating variables $\mathbf{h} = (v, w)$

average transient lifetime increases exponentially with system size



T. Lilienkamp et al., Phys. Rev. Lett. 119 (2017)

T. Lilienkamp and U. Parlitz, Phys. Rev. Lett. 120 (2018)

Can we predict the end of the chaotic transient?

No, not yet :-)

But during a period of time close to the end of the transient the system responds differently to external perturbations. *Prediction possible ??*

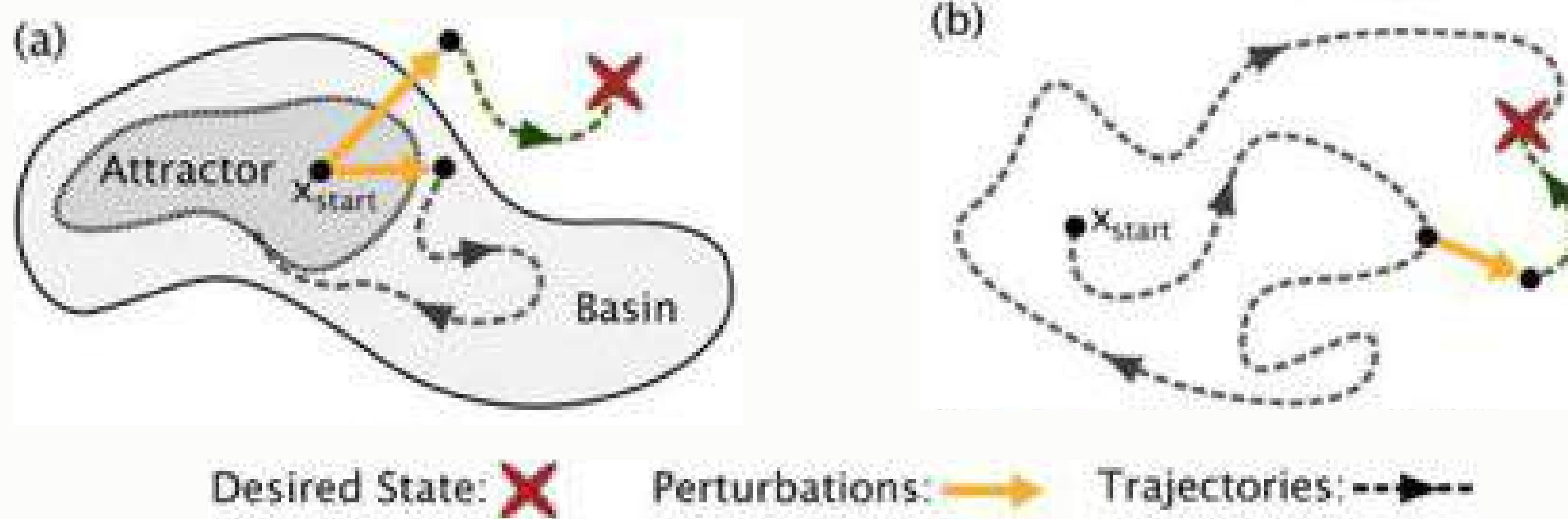
T. Lilienkamp and U. Parlitz, PRL 120 (2018); PRE 98 (2018); PRE 102 (2020)

We can, however, predict the average transient lifetime from observable quantities like:

- dominant frequency
- excitable gap
- (pseudo) ECG
- shape of the action-potential- duration (APD) curve
- no. of phase singularities

Potential Implications of Transient Chaos for Defibrillation

Persistent chaos vs. Transient chaos



control: kick state into basin of another attractor

minimal perturbation strength required

kick state to neighbouring orbit with (much) shorter transient time

can be achieved with (very) small perturbations

Controlling Transient Chaos

Terminating spiral wave chaos with few single perturbations

Fenton-Karma model

$$\frac{\partial u}{\partial t} = \nabla \cdot \underline{\mathbf{D}} \nabla u - I_{Ion}(u, \mathbf{h})/C_m$$

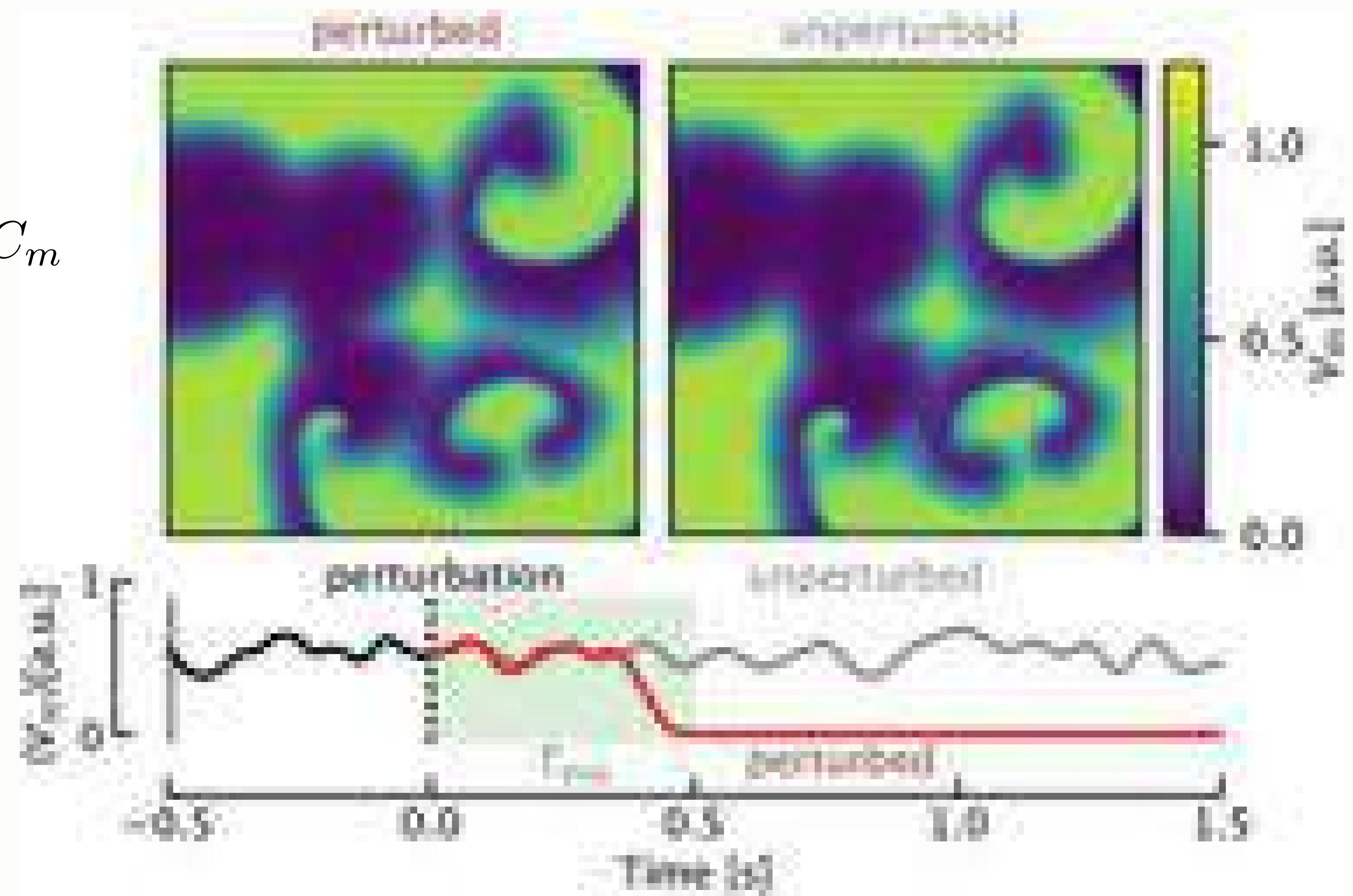
$$\frac{\partial \mathbf{h}}{\partial t} = \mathbf{g}(u, \mathbf{h})$$

gating variables $\mathbf{h} = (v, w)$

$T_{evo} = 500$ ms

T. Lilienkamp and U. Parlitz,
Chaos 30, 051108 (2020)

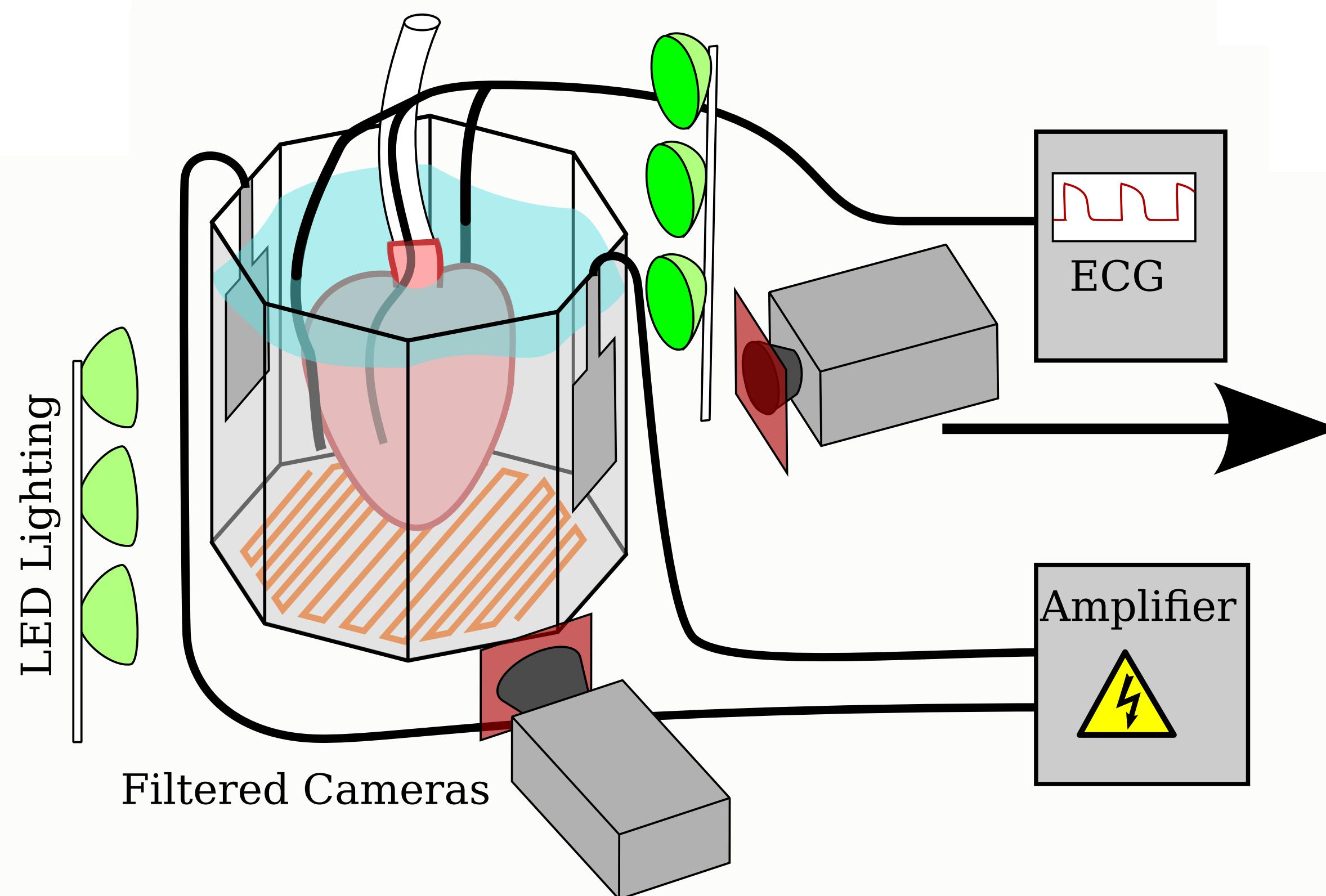
S. P. Cornelius et al., Nat. Commun. 4, 2939 (2013)



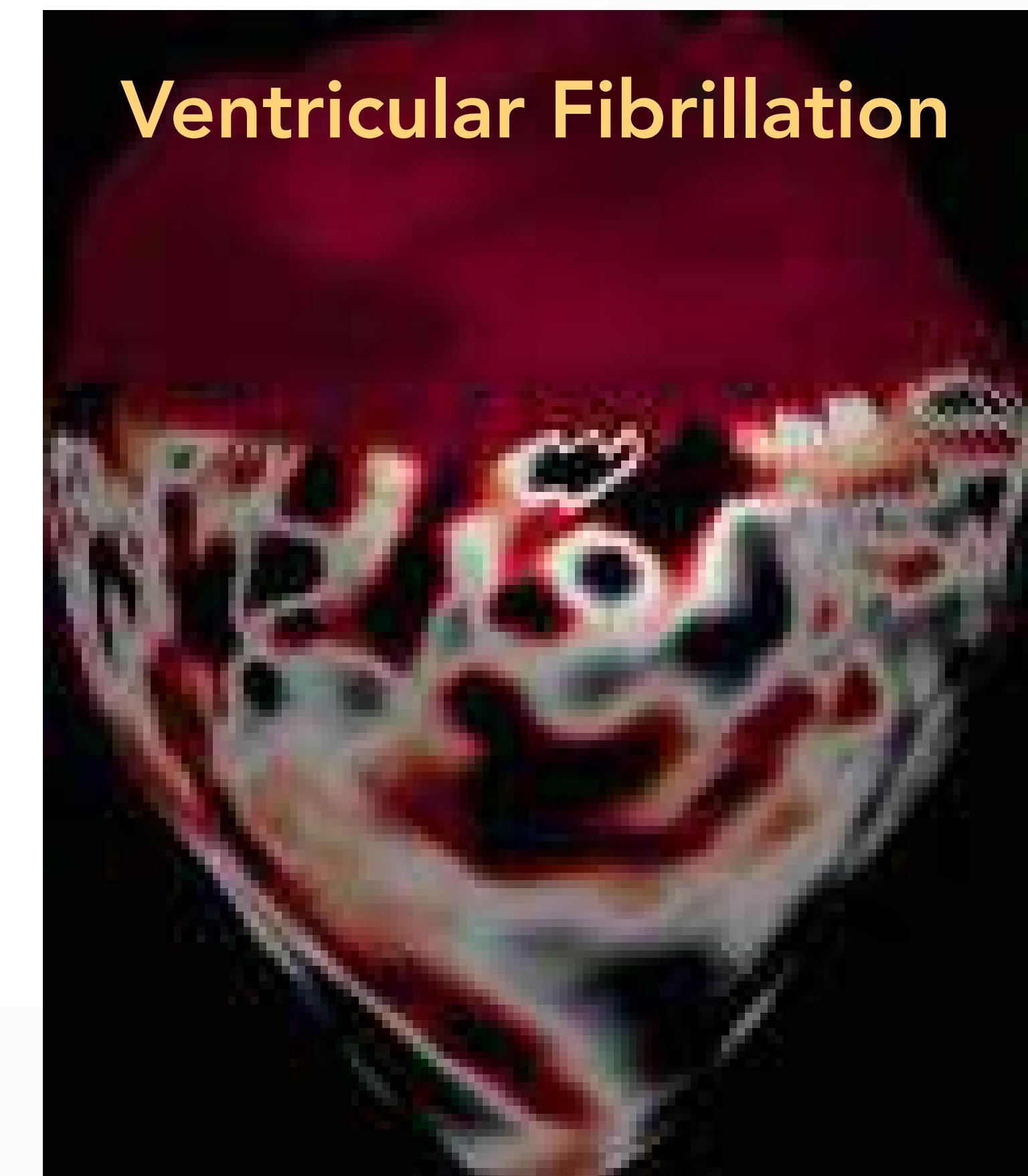
Measuring Cardiac Dynamics

Optical mapping in Langendorff perfusion system

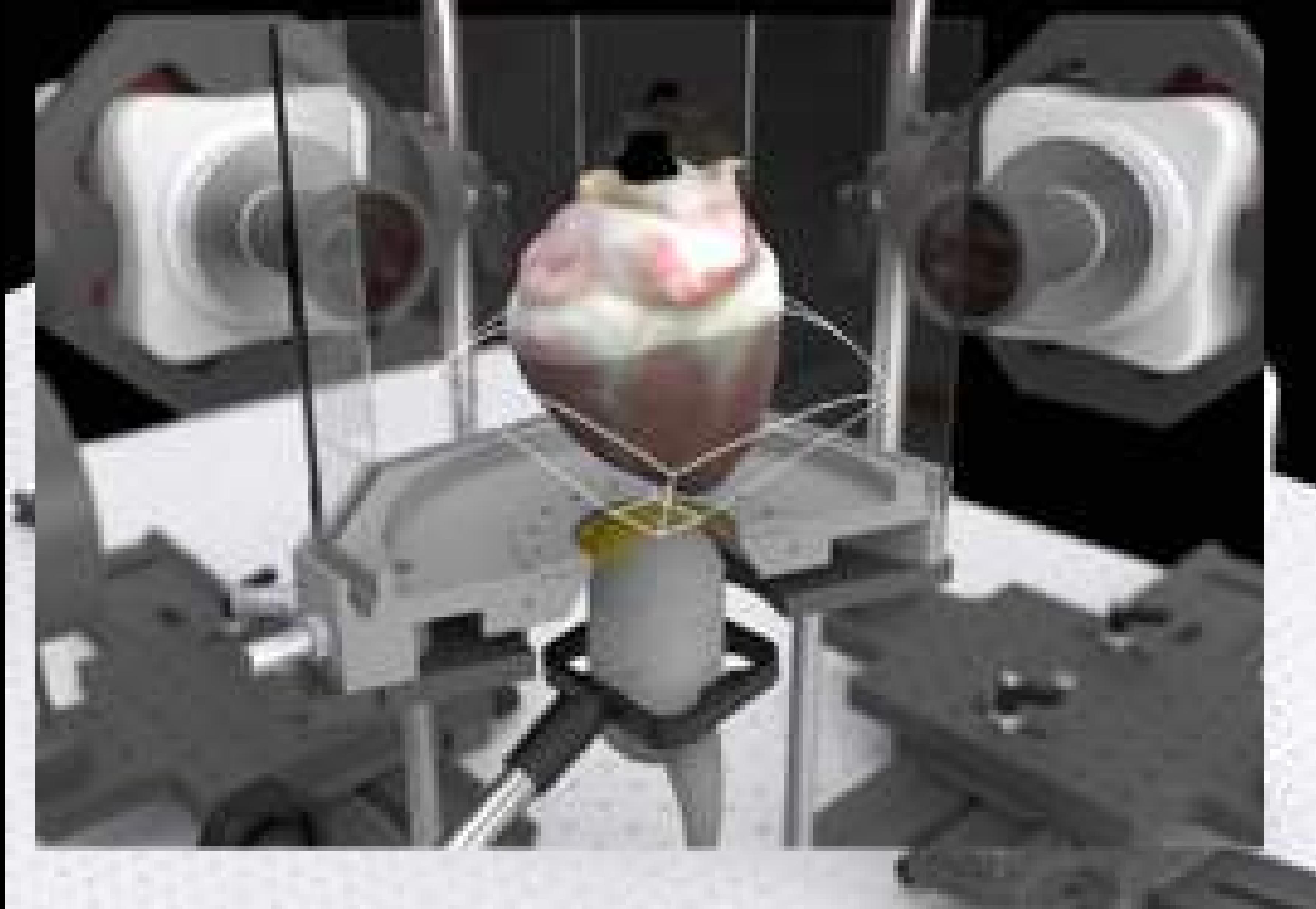
Visualisation of **membrane voltage** and **Ca⁺ concentration** on the **surface of the heart** using **fluorescent dyes**



J. Schröder-Schelting



Simultaneous Optical Mapping and 4D Ultrasound



Visualizing mechanical scroll waves within the heart muscle using highspeed ultrasound

Mechanical
Filament

Acuson SC2000
(Siemens Inc.),
Transducer 4Z1c,
2.8 MHz,
134 vps,
0.5 mm

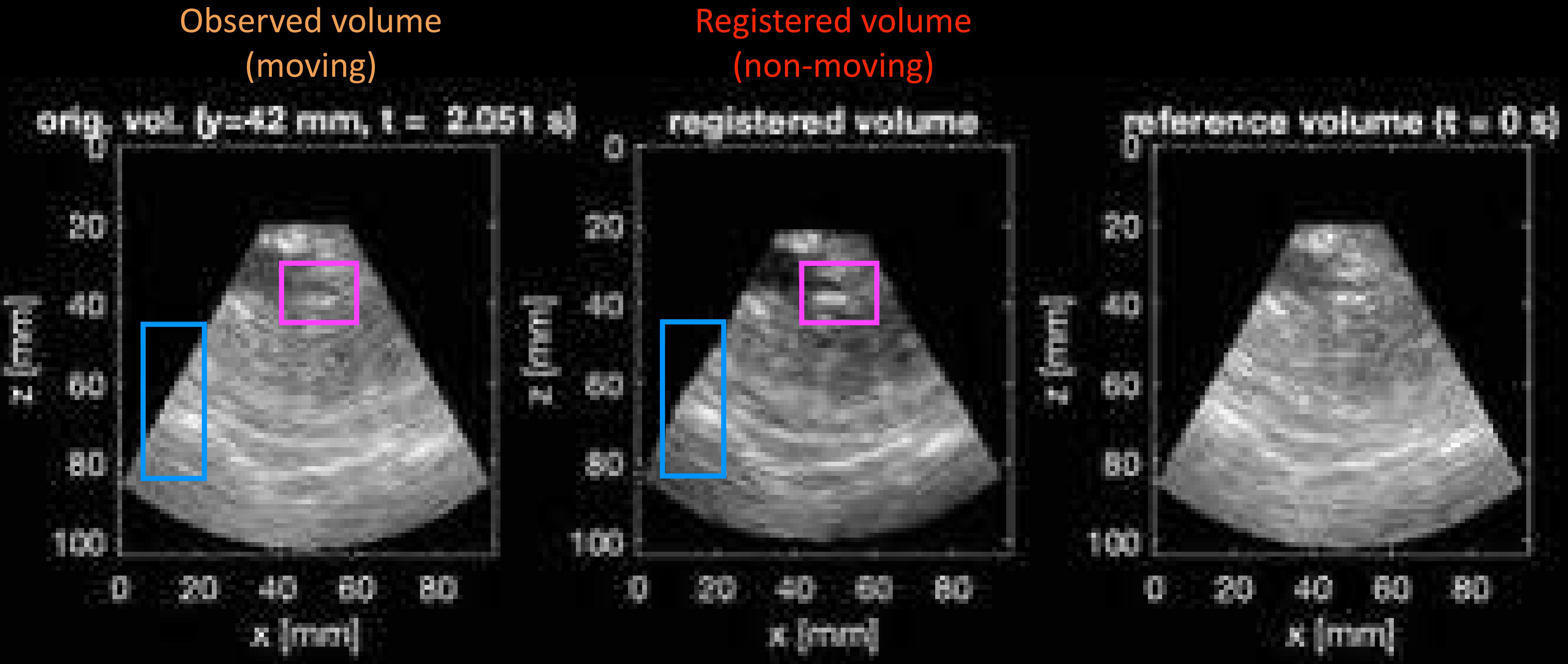
1 cm



J. Christoph et al.
Nature (2018)

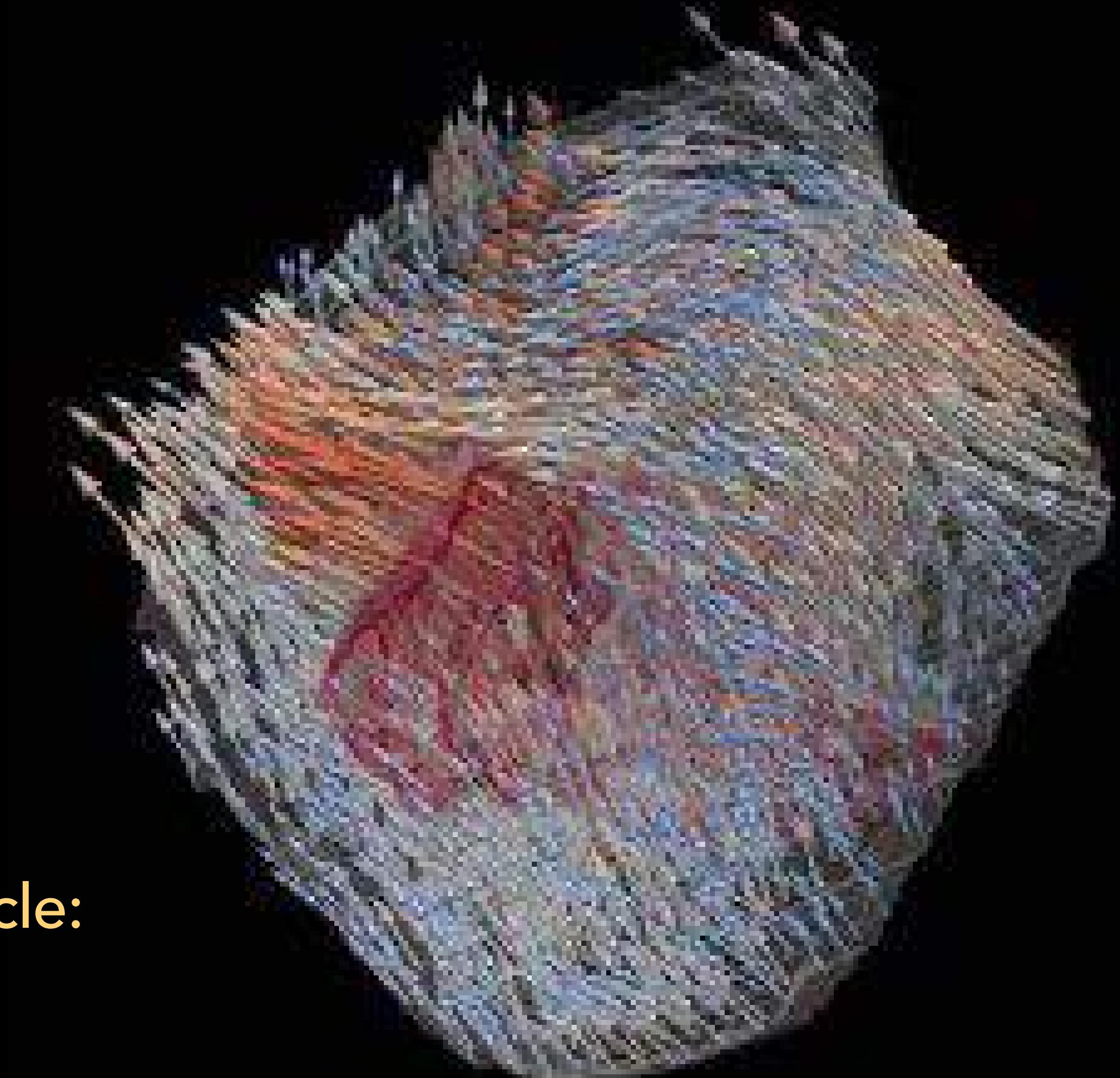
Ultrasound imaging of a human heart during by-pass surgery

Motion analysis estimates a **3D displacement vector field** that describes the motion of the tissue



Motion tracking in high-resolution 4D ultrasound resolves mechanical motion during ventricular fibrillation

ultrasound device



First observation of mechanical scroll waves within the heart muscle:
J. Christoph et al. Nature 555 (2018)

Data driven modelling in cardiac research

- prediction of future evolution (e.g., membrane voltages, mechanical motion)
- extraction of relevant features from (noisy) raw data → classification
- cross estimation of observables that are difficult to measure directly (e.g. electrical activity inside the heart muscle)

Methods for spatio-temporal timeseries:

- nearest neighbours prediction using reconstructed local states
J. Isensee et al., J. of Nonlin. Sci. 30, 713–735 (2020)
- echo state networks (reservoir computing)
R.S. Zimmermann and U. Parlitz, Chaos 28, 043118 (2018); S. Herzog et al., Frontiers in Appl. Math. and Statistics 6, 616584 (2021)
- convolutional neural networks
S. Herzog et al., Front. in Appl. Math. and Stat. 4, 60 (2018); Chaos 29, 123116 (2019); R. Stenger et al., (under review)

Prediction of future evolution of membrane voltage

Data Driven Modeling of Spatio-Temporal Systems

Model to generate training and test data: The Bueno-Orovio-Cherry-Fenton model

A. Bueno-Orovio et al., J. Theor. Biol. 253 (2008)

PDEs describing electrical excitation waves in cardiac tissue

$$\frac{\partial u}{\partial t} = D \cdot \nabla^2 u - (J_{si} + J_{fi} + J_{so})$$

**u membrane potential
to be predicted**

$$\frac{\partial v}{\partial t} = \frac{1}{\tau_v^-} (1 - H(u - \theta_v)) (v_\infty - v) - \frac{1}{\tau_v^+} H(u - \theta_v) v$$

$$\frac{\partial w}{\partial t} = \frac{1}{\tau_w^-} (1 - H(u - \theta_w)) (w_\infty - w) - \frac{1}{\tau_w^+} H(u - \theta_w) w$$

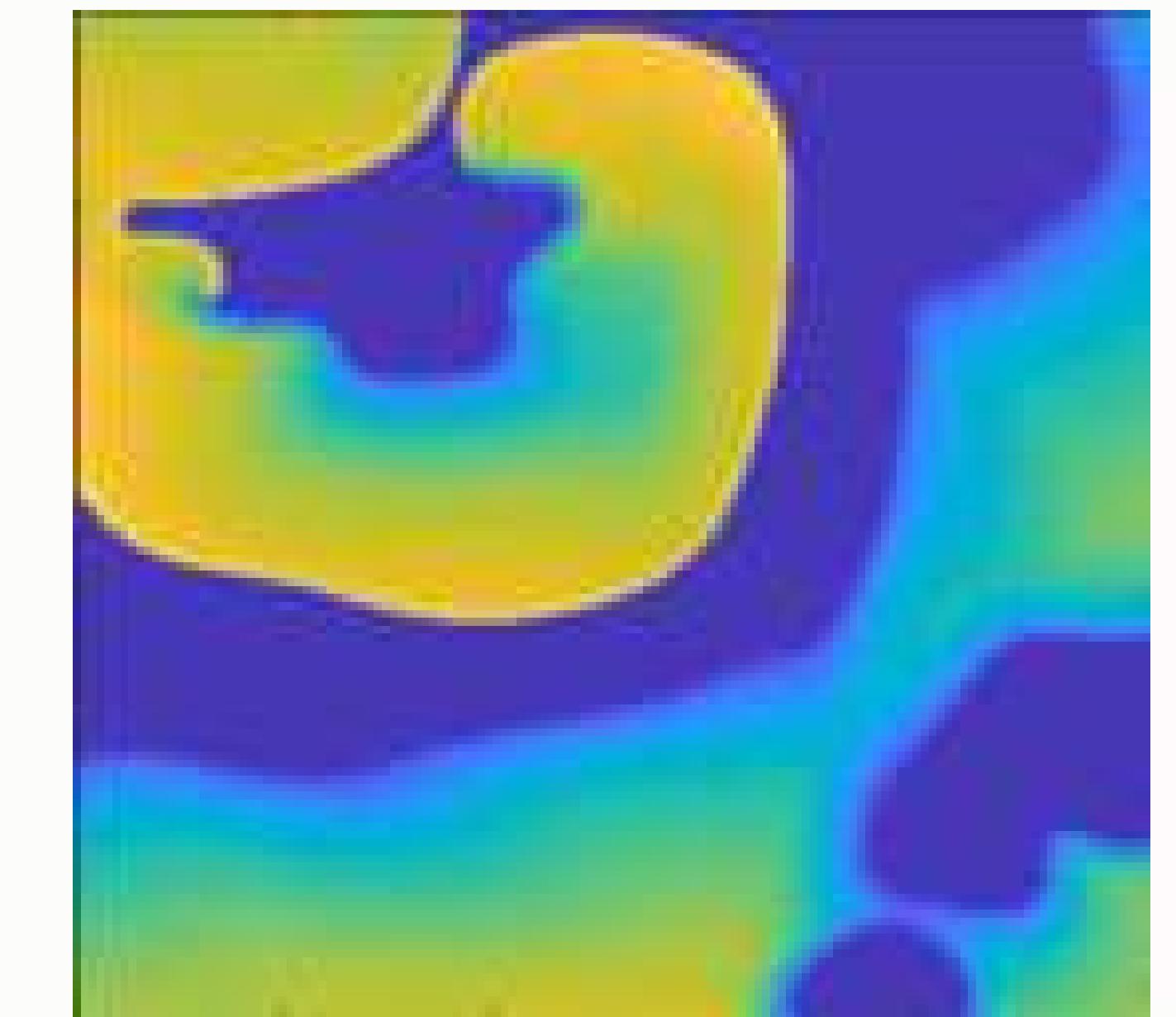
$$\frac{\partial s}{\partial t} = \frac{1}{2\tau_s} ((1 + \tanh(k_s(u - u_s))) - 2s)$$

with ionic currents:

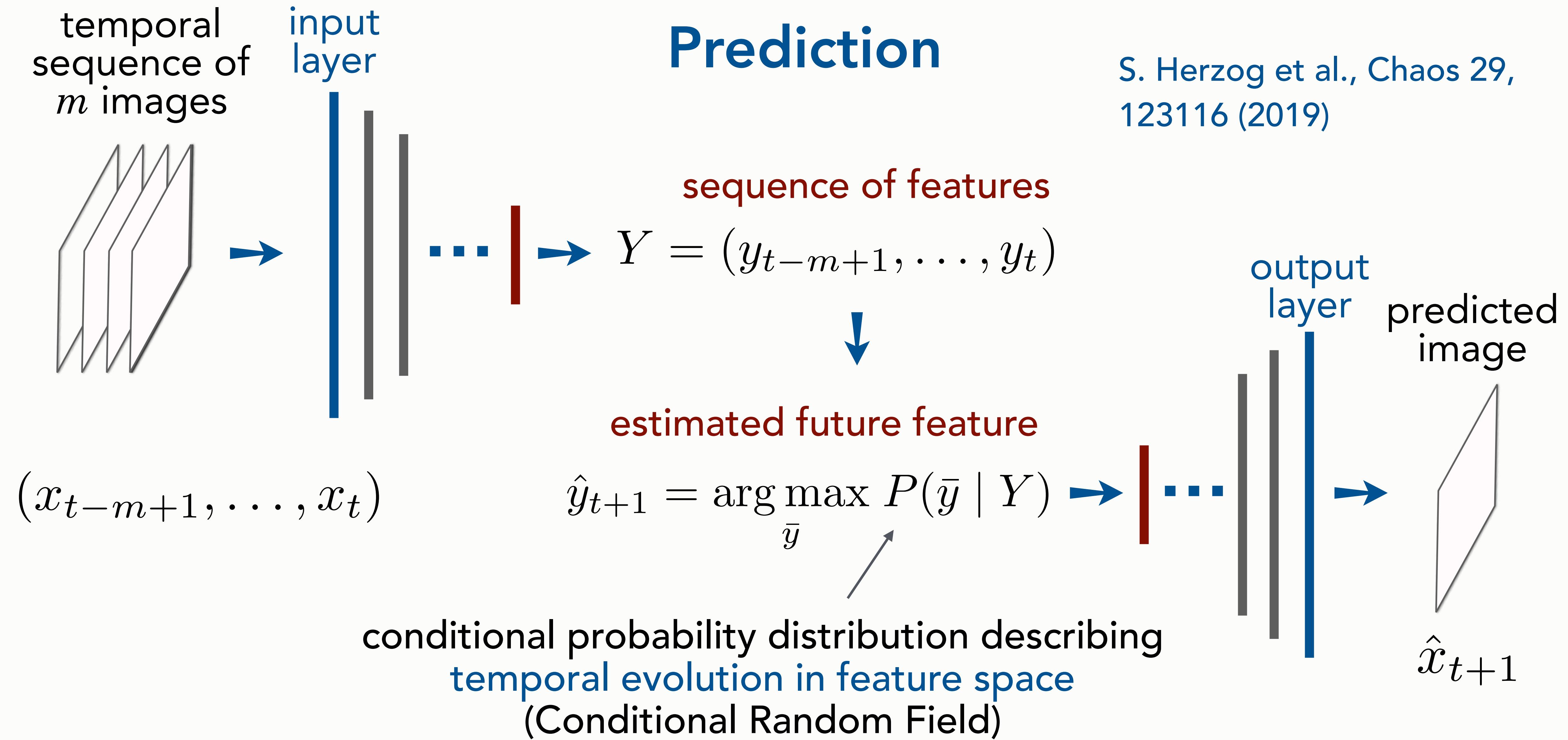
$$J_{si} = -\frac{1}{\tau_{si}} H(u - \theta_w) ws$$

$$J_{fi} = -\frac{1}{\tau_{fi}} v H(u - \theta_v) (u - \theta_v) (u_u - u)$$

$$J_{so} = \frac{1}{\tau_o} (u - u_o) (1 - H(u - \theta_w)) + \frac{1}{\tau_{so}} H(u - \theta_w)$$



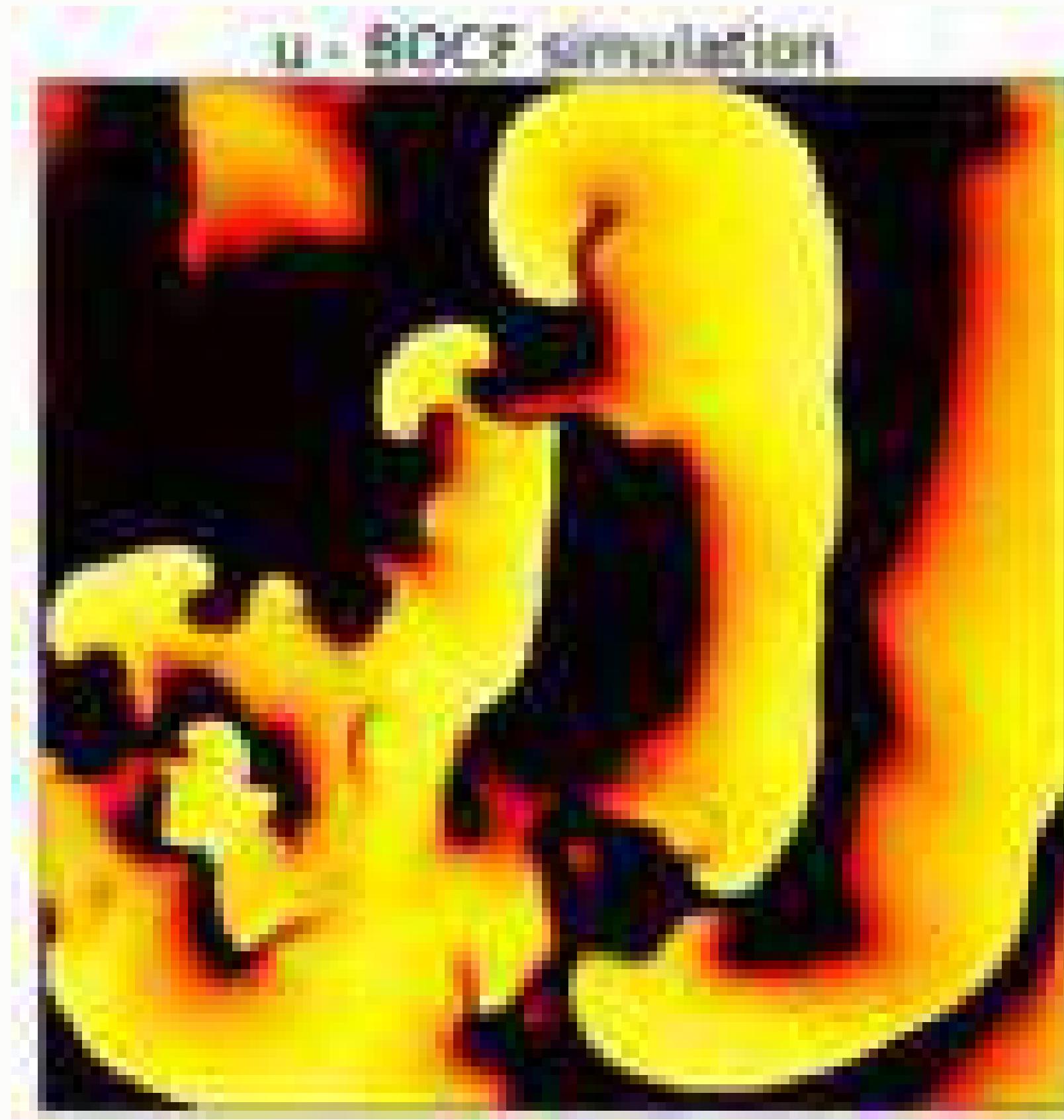
Convolutional Auto-Encoder



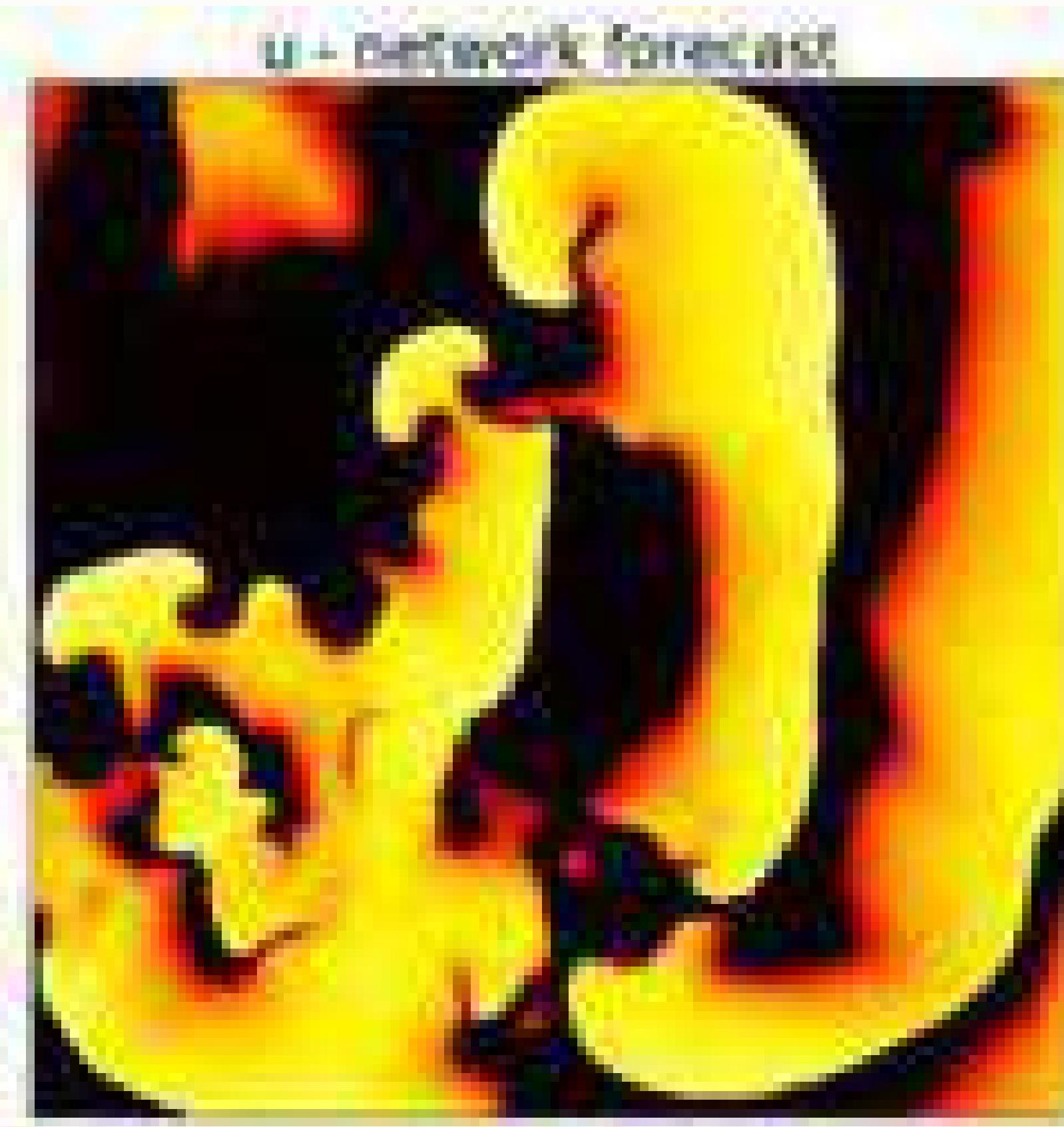
Convolutional Auto-Encoder

Iterated Forecasting of $u(t)$

true



forecast



difference



good for 5 spiral rotations

S. Herzog et al., Frontiers in Appl. Math. and Statistics 4, 60 (2018)

Convolutional Auto-Encoder

Prediction of Kuramoto-Sivashinsky Dynamics

$$\frac{\partial u}{\partial t} + \frac{\partial^2 u}{\partial x^2} + \frac{\partial^4 u}{\partial x^4} + \left| \frac{\partial u}{\partial x} \right|^2 = \mu \cos\left(\frac{2\pi x}{\lambda}\right)$$

$$\mu = 0.01$$

largest Lyapunov exponent

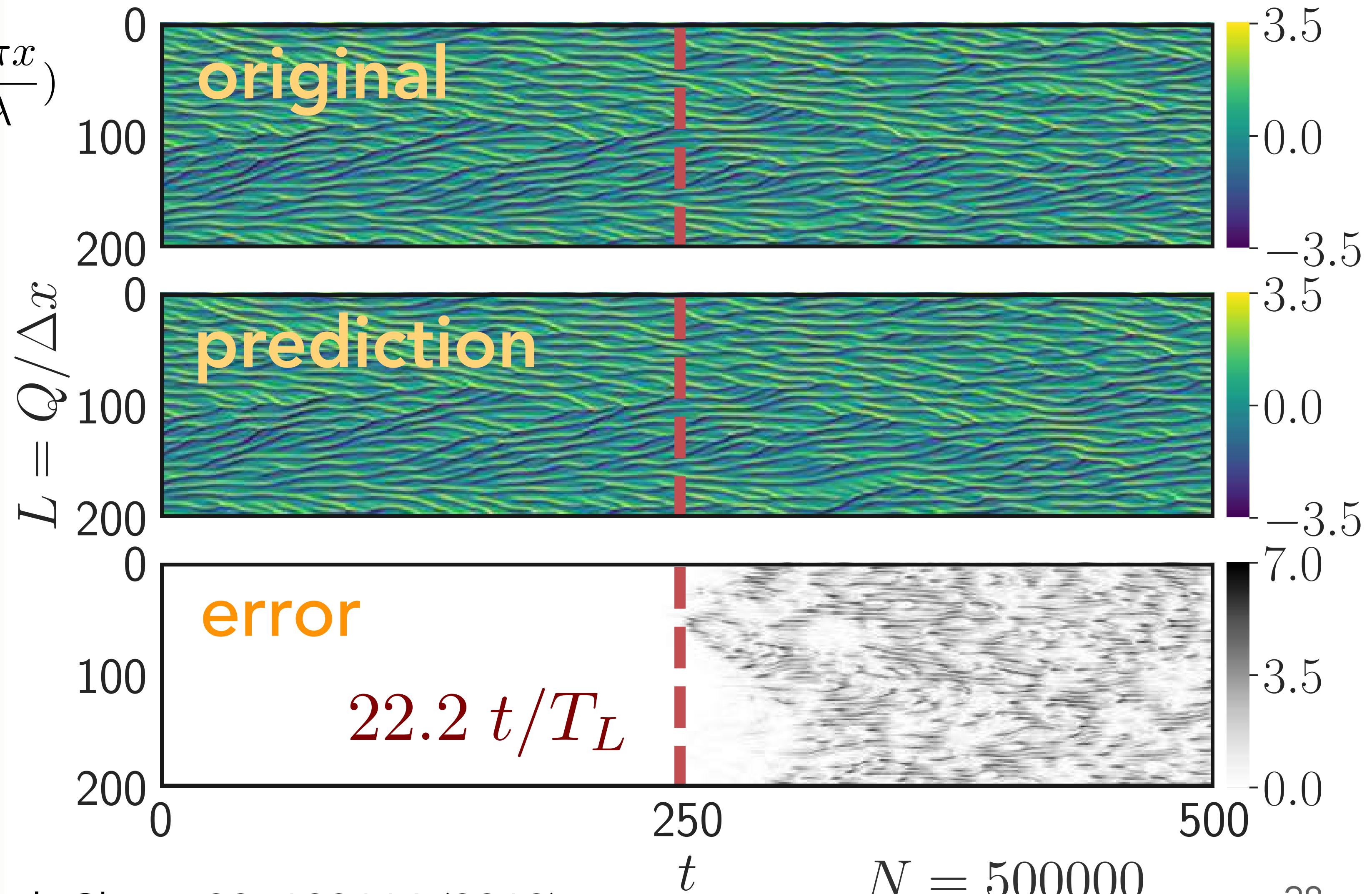
$$\Lambda_{max} = 0.09$$

Lyapunov time

$$T_L = \frac{1}{\Lambda_{max}} = 11.1$$

J. Pathak et al.,
Phys. Rev. Lett. 120 (2018)

$$L = 120 : \approx 4\Lambda t$$



Data Driven Modeling in Cardiac Dynamics

Cross estimation tasks:

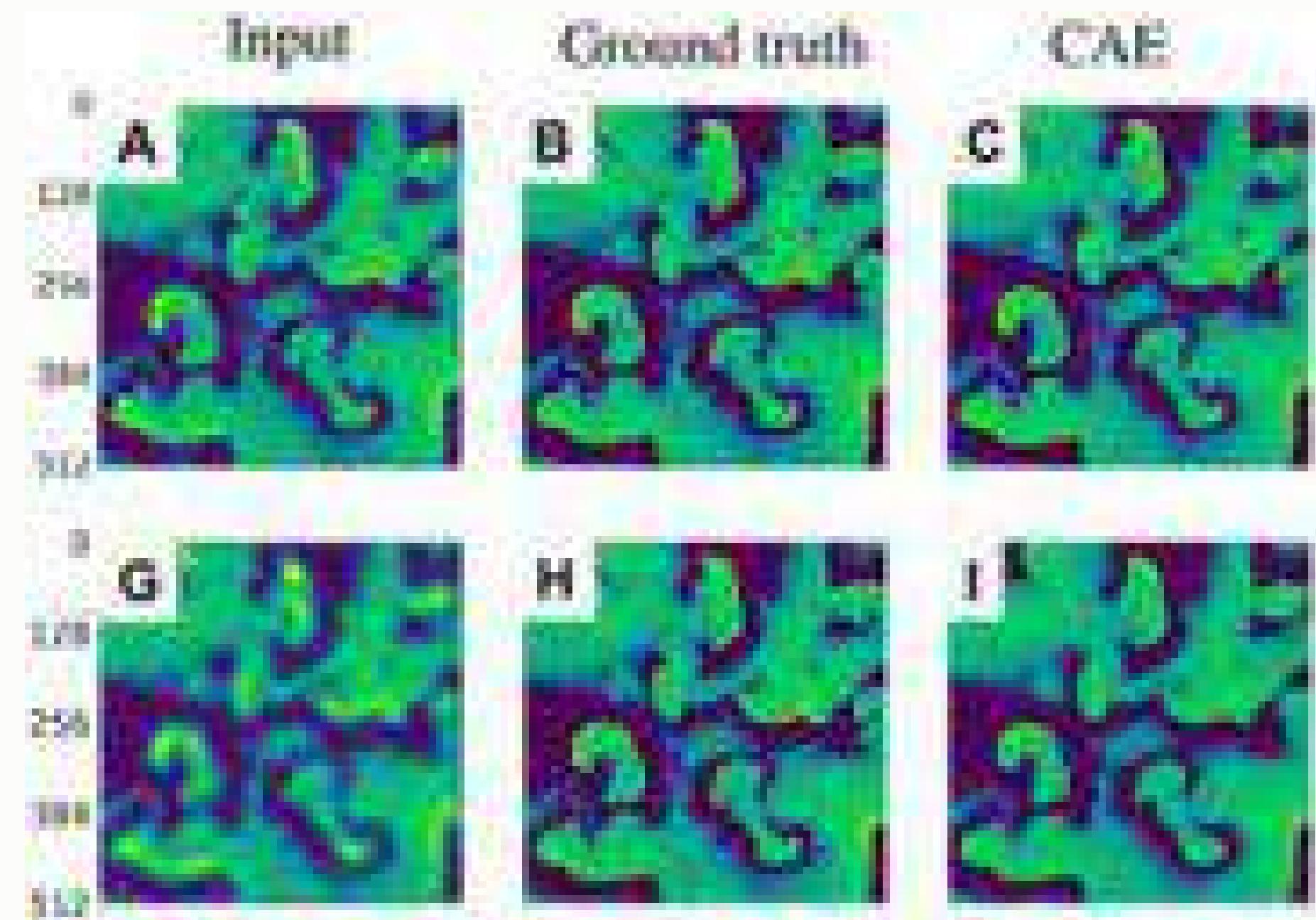
- recovering complex wave patterns from impaired observations (e.g. noise)
- cross-predicting electrical excitation from mechanical contraction
- predicting electrical excitation waves *inside* the heart muscle from observations on the *surface*

Data Driven Modeling of Spatio-Temporal Systems

Recovering Complex Wave Patterns From Impaired Observations

Reconstruct original data from **noisy**, **blurred** or **undersampled** data.

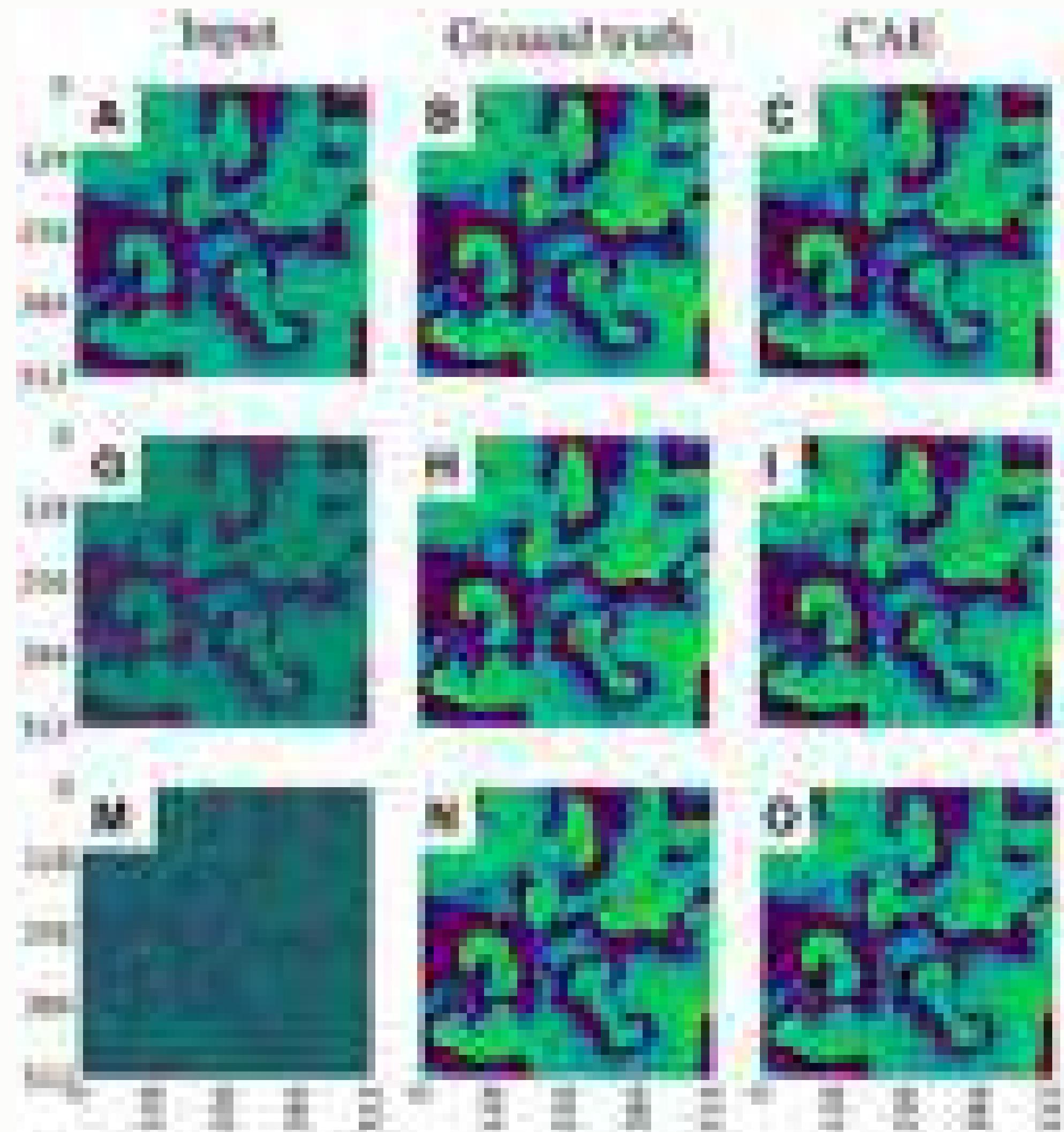
blurred:



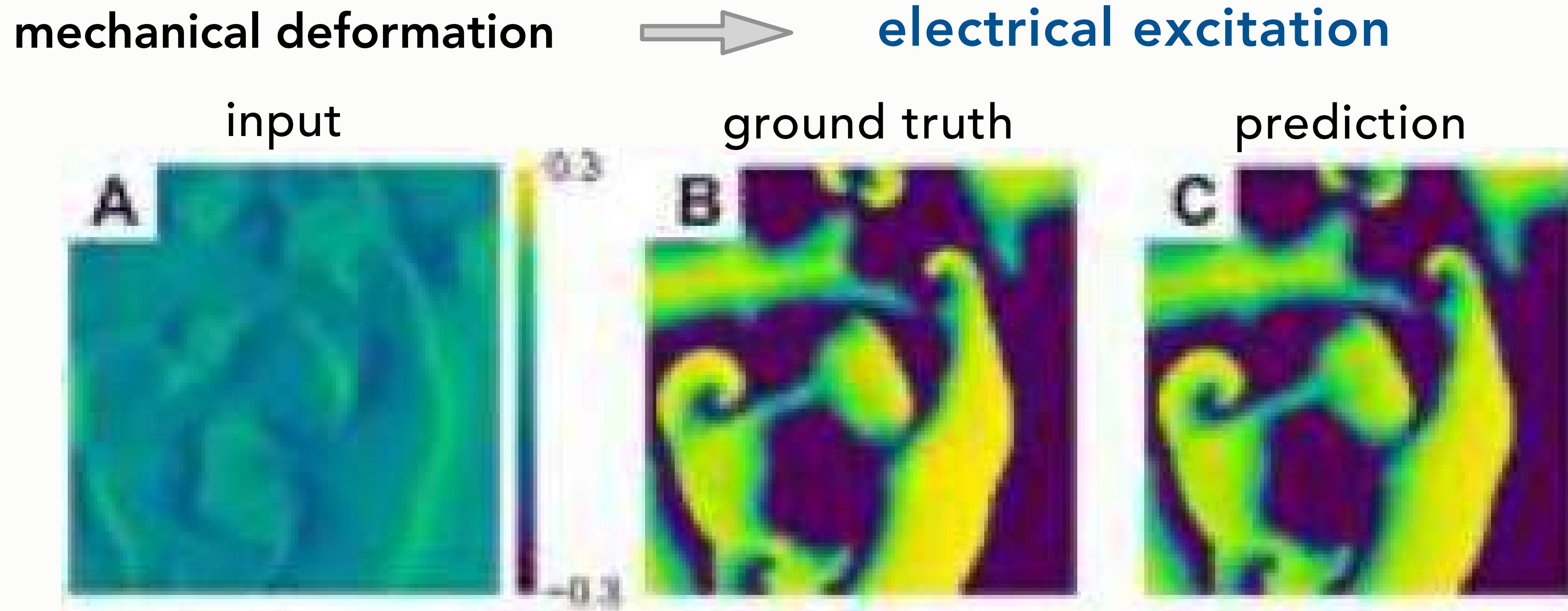
CAE = convolutional autoencoder

S. Herzog et al., Frontiers in Appl. Math. and Statistics 6, 616584 (2021)

noisy:



Electrical excitation from mechanical deformation



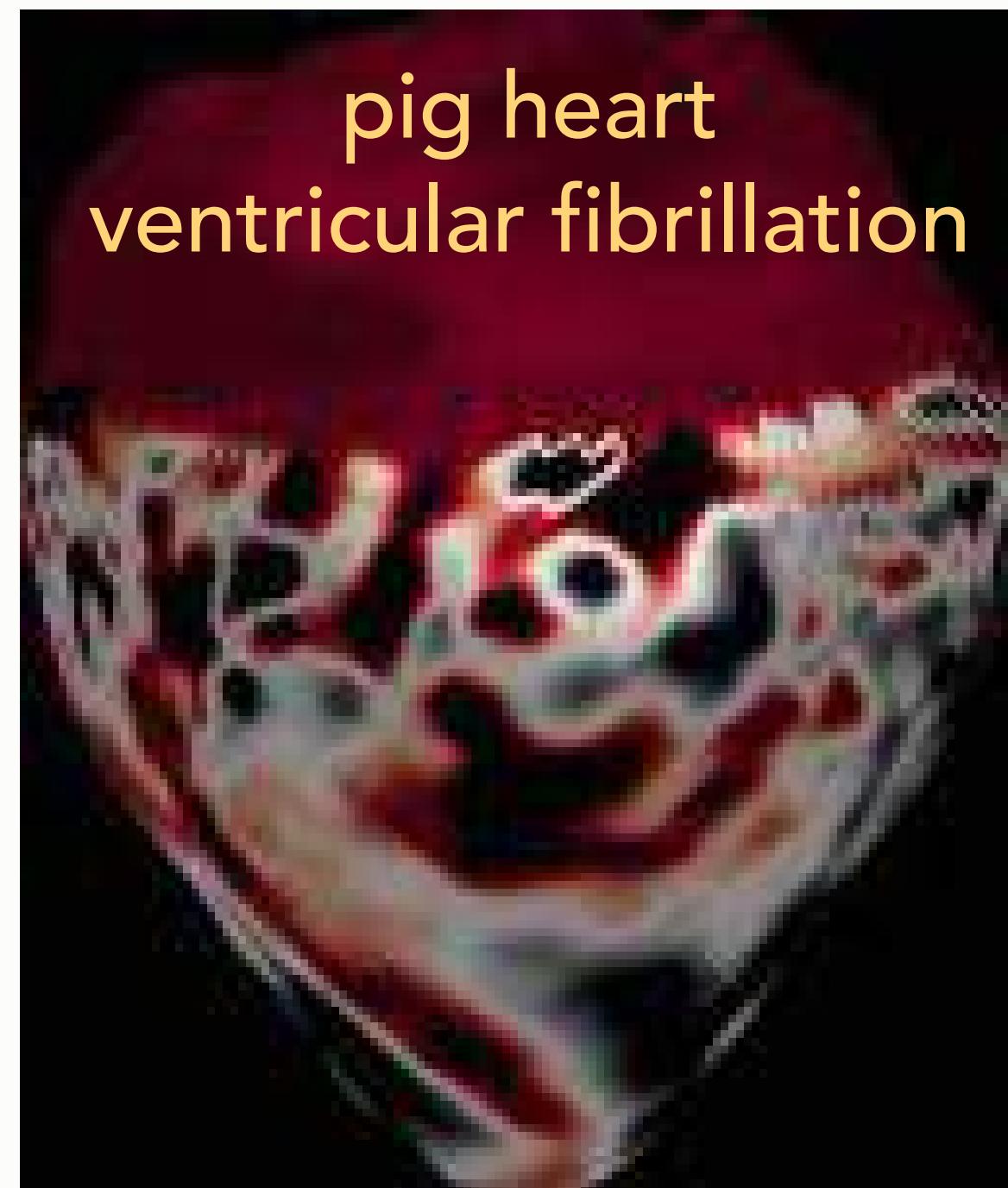
Data generated by a conceptual electro-mechanical model (BOCF model driving a mass-spring system)
Convolutional Auto-encoder; Reservoir Computing

S. Herzog et al., Frontiers Appl. Math. Stat. 6 (2021) ; J. Christoph and J. Lebert, Chaos 30 (2020)

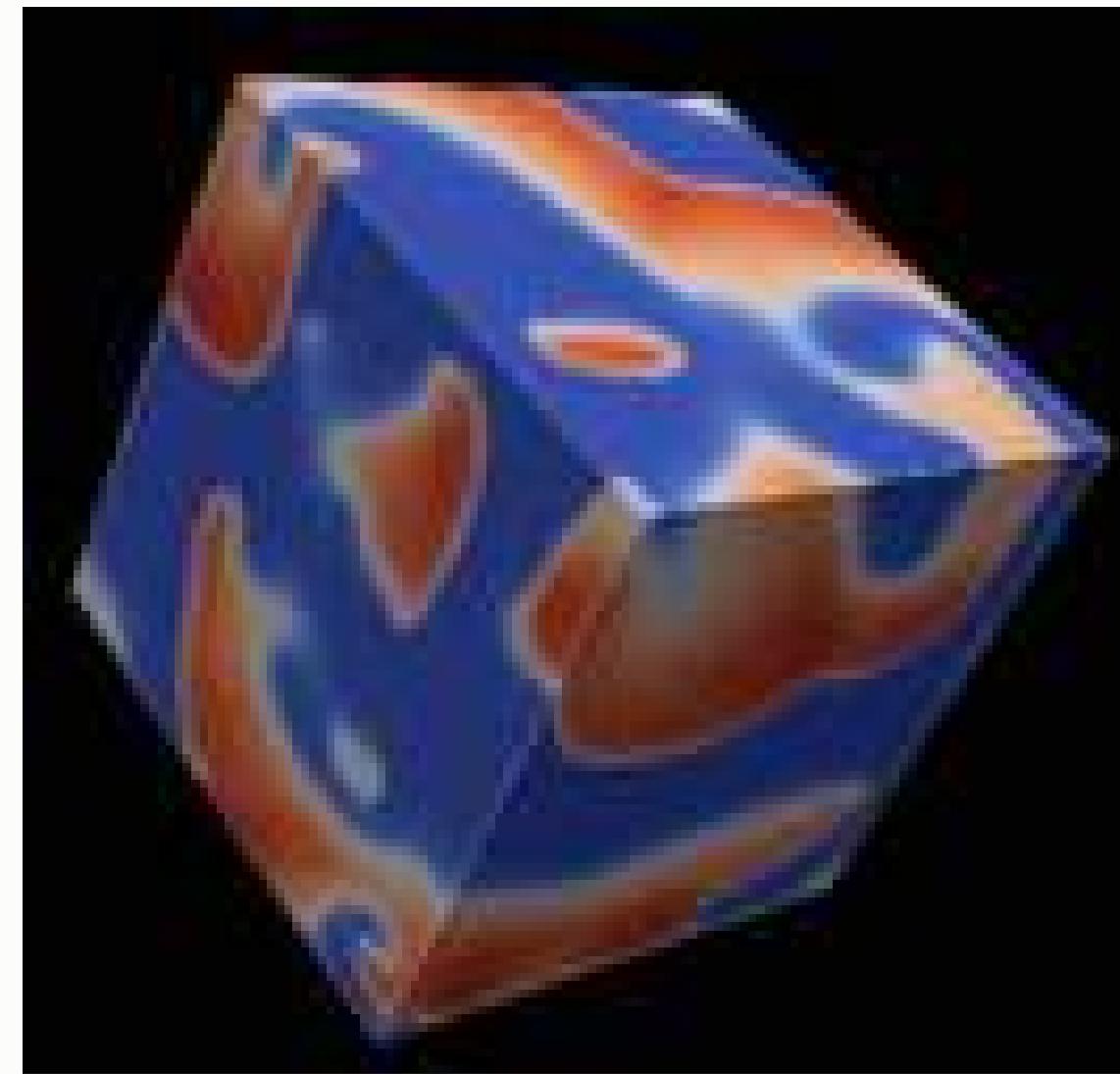
Data Driven Modeling

From the surface into the depth

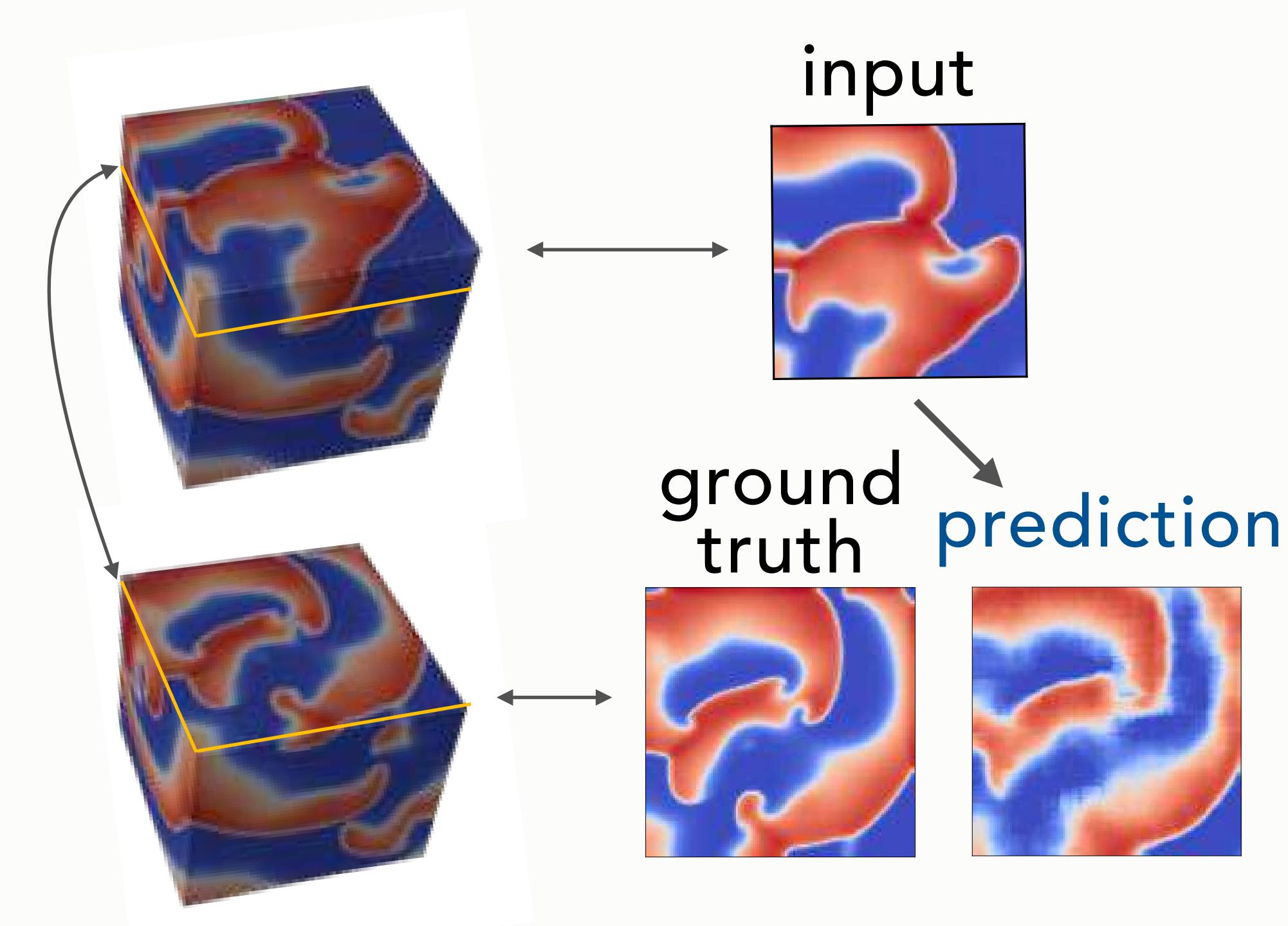
optical mapping using voltage sensitive dyes provides electrical excitation waves **only on the surface of the heart**



simulation of a 3D excitable medium



predict activity in deeper layers using Convolutional Neural Network



Inga Kottlarz

Data Driven Modeling

From Surface To Depth

3D Barkley model

$$\frac{du}{dt} = D\nabla^2 u + \frac{1}{\varepsilon}u(1-u)\left(u - \frac{v+b}{a}\right)$$

$$\frac{dv}{dt} = u^3 - v$$

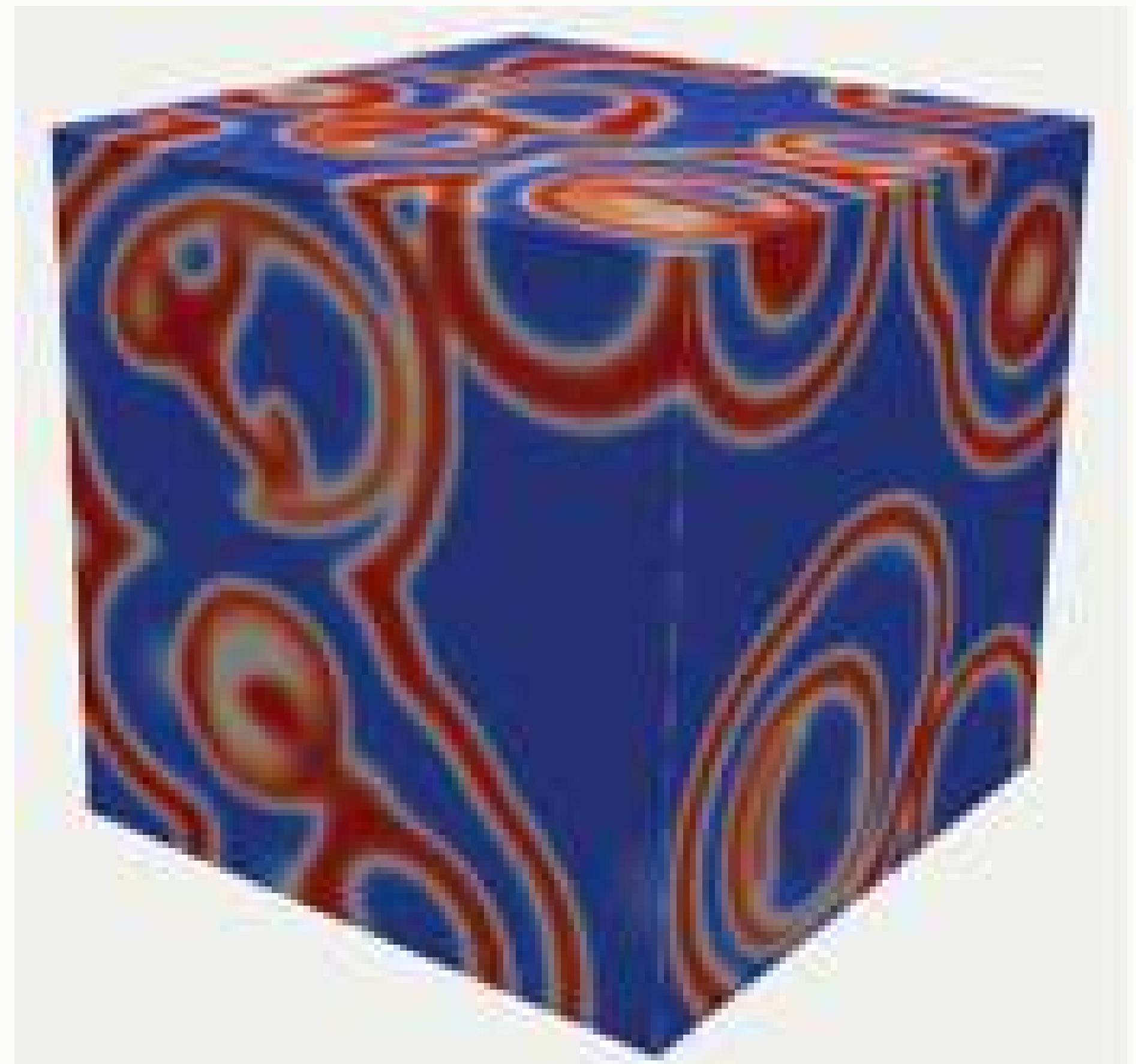
$$a = 0.75 \quad b = 0.06 \quad \varepsilon = 0.08 \quad D = 0.02$$

grid: $120 \times 120 \times 120$

predict deeper layers from data at surface

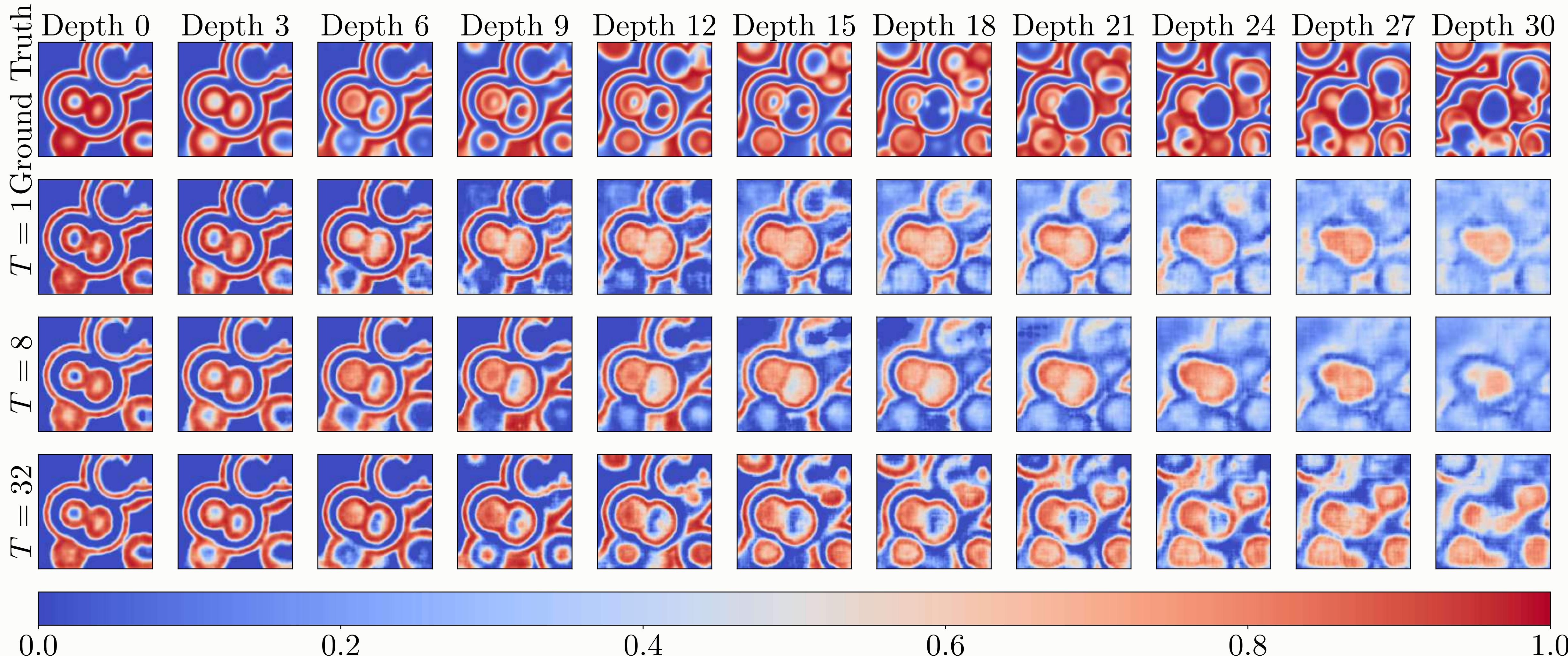
using convolutional neural networks:

Auto-Encoder, Spatio-Temporal LSTM, Diffusion Model



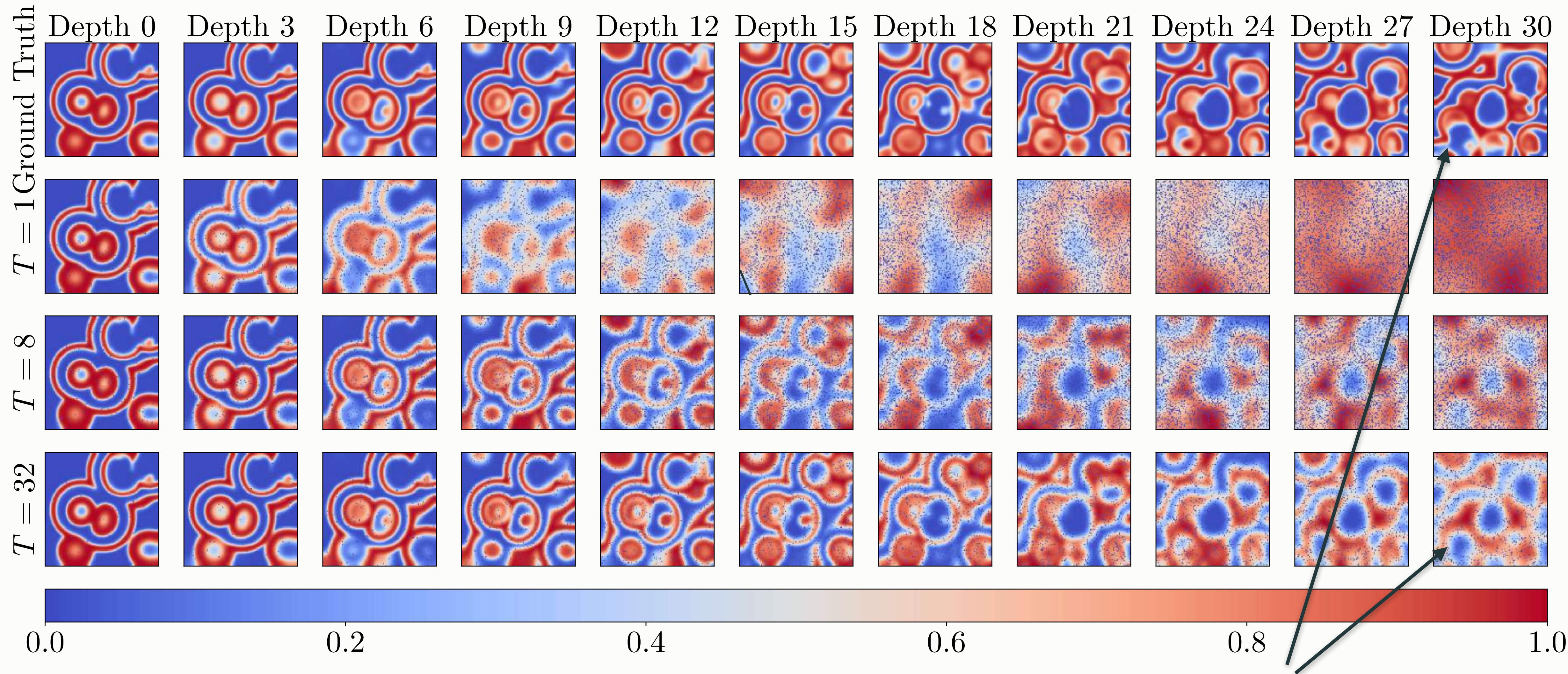
From the surface into the depth

Reconstruction using Autoencoder with different input lengths $T \in \{1, 8, 32\}$



From the surface into the depth

Reconstruction using diffusion model with different input lengths of $T \in \{1, 8, 32\}$

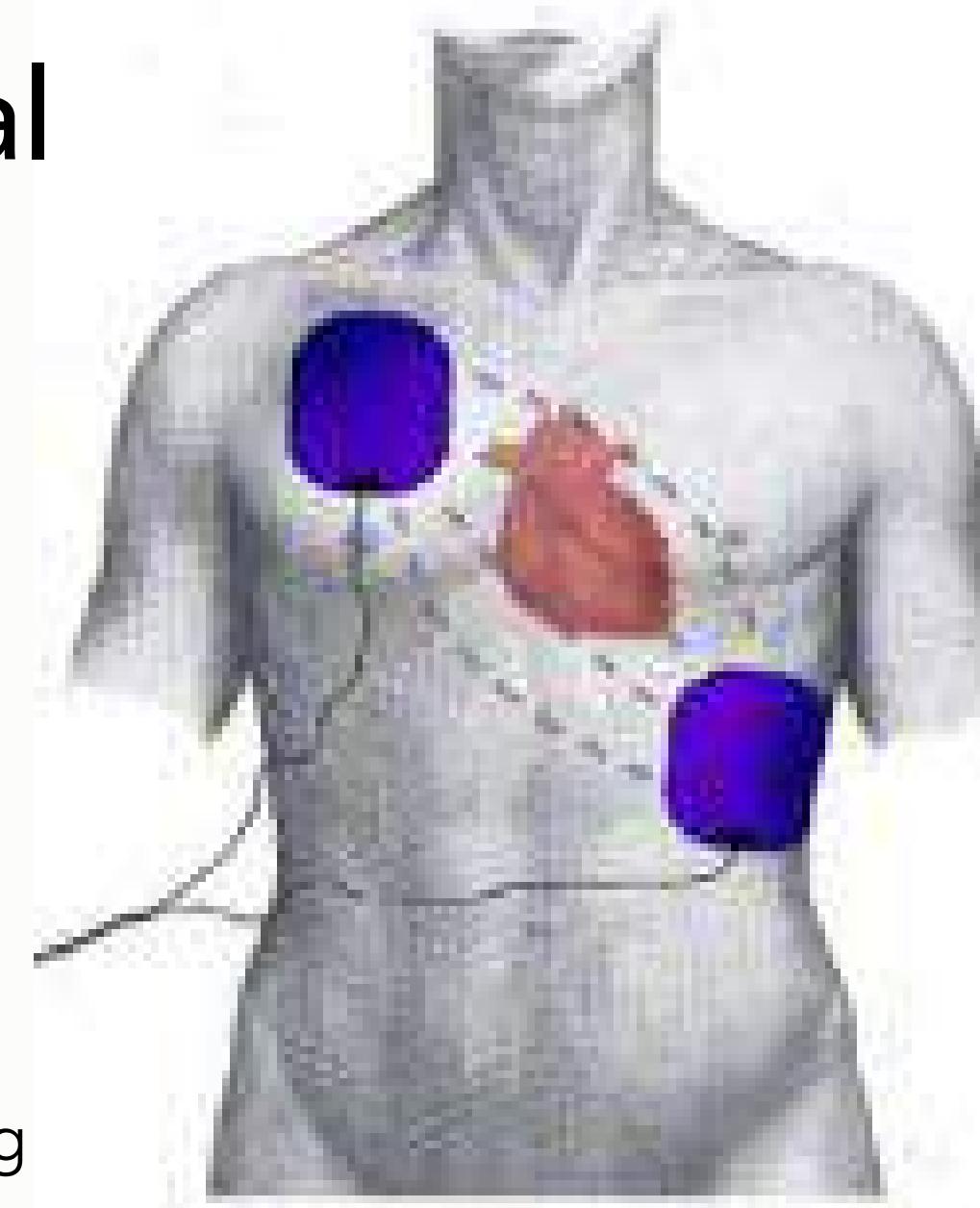


Terminating cardiac arrhythmias

Defibrillation

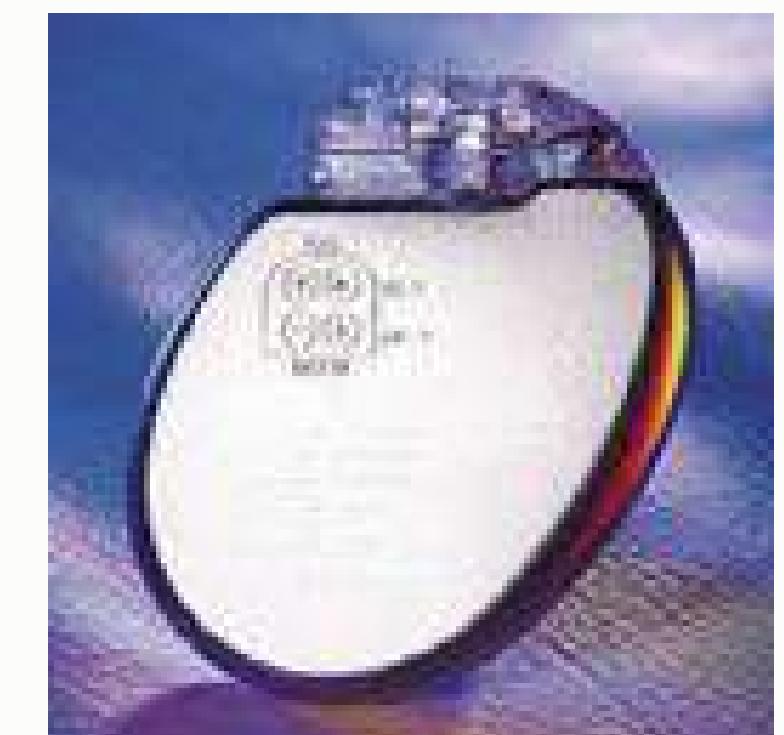
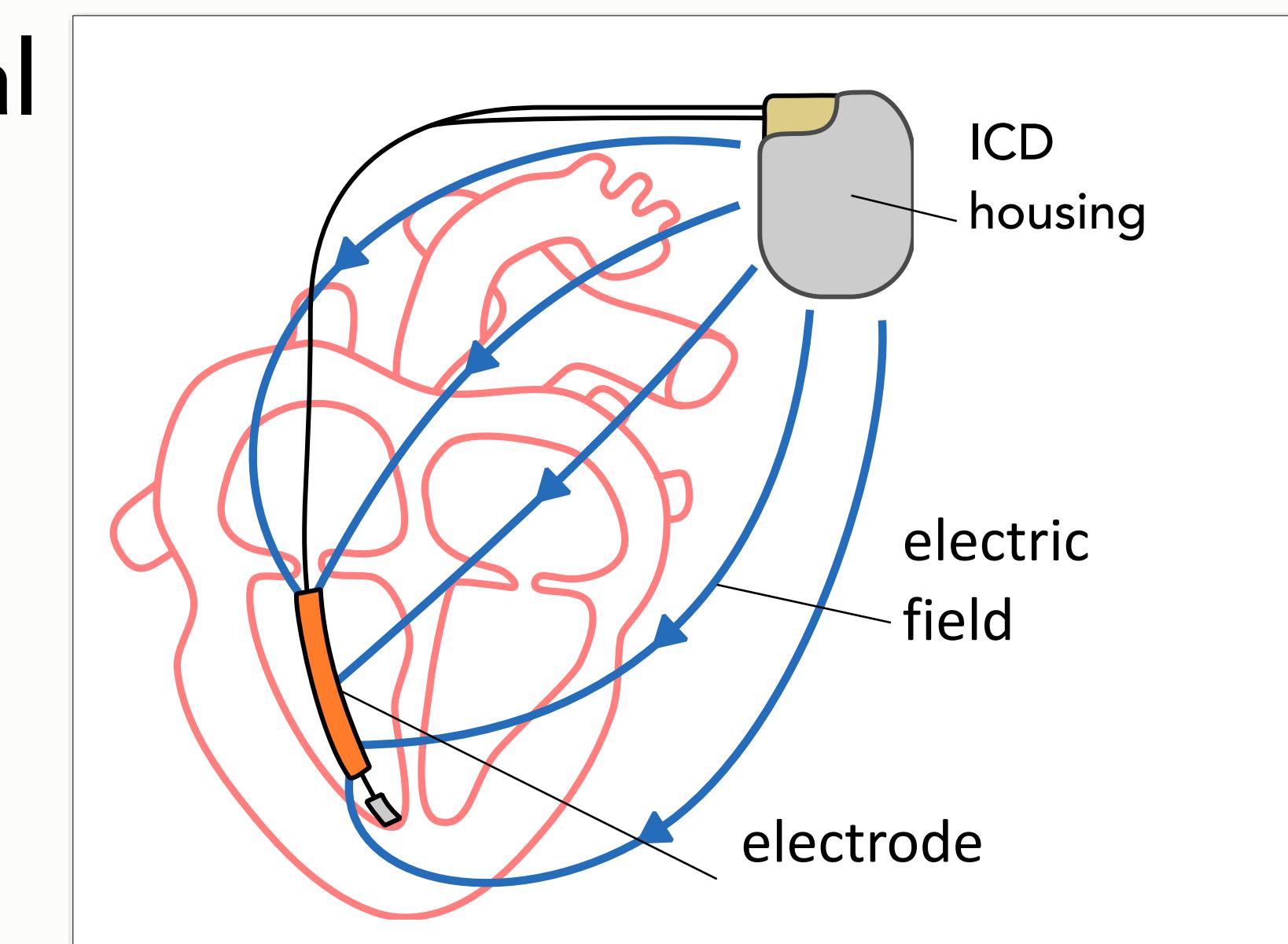
Principle: Reset electrical activity of all cells by synchronous excitation

external



PhilippN
wikimedia.org

internal



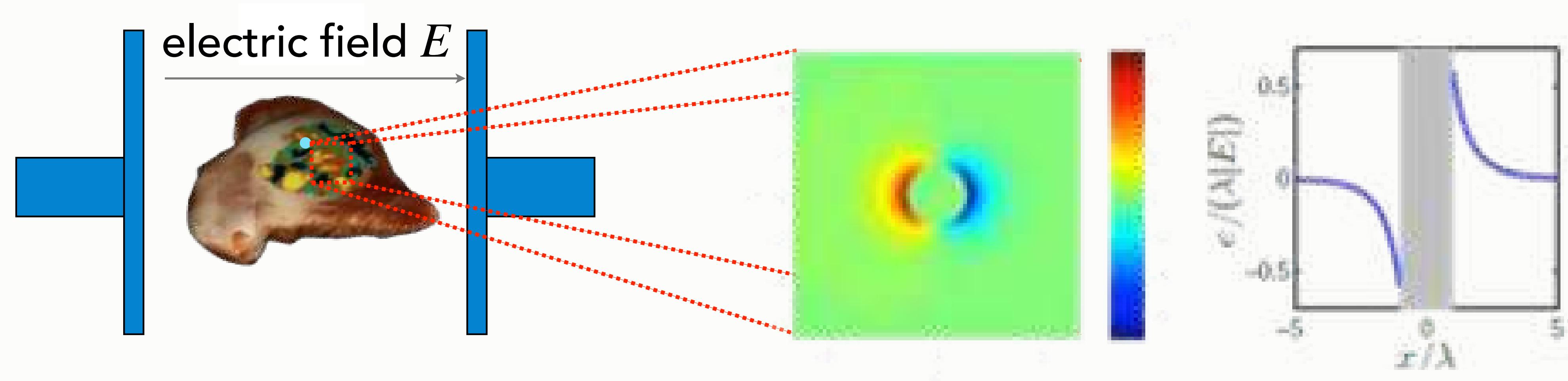
1000 V 20 A 12ms → 240 J

400 V 8 A 12 ms → 40J

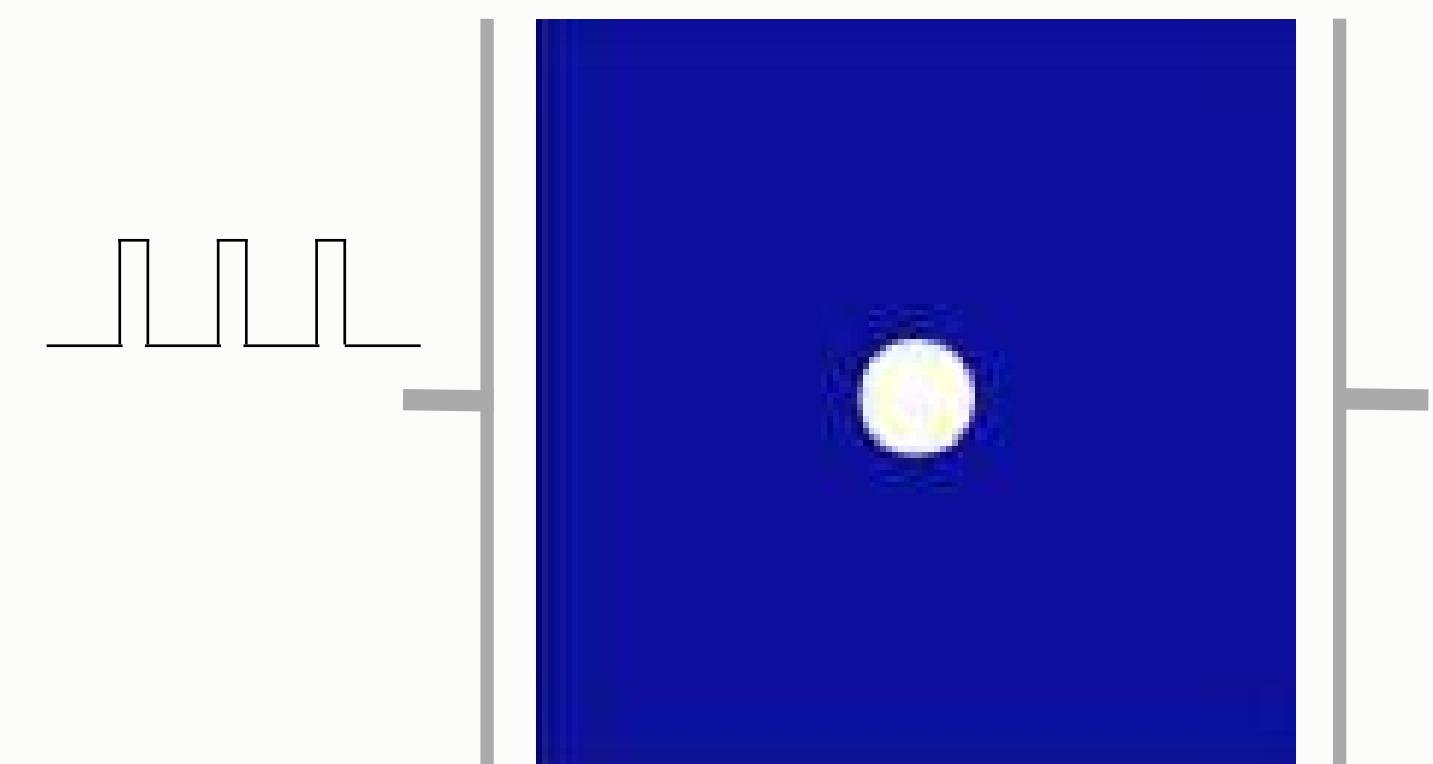
Severe side effects: tissue damage - traumatic pain G.P. Walcott et al., Resuscitation 59 (2003)

Conduction heterogeneities act as virtual electrodes

blood vessels, scars, fatty tissue, ...



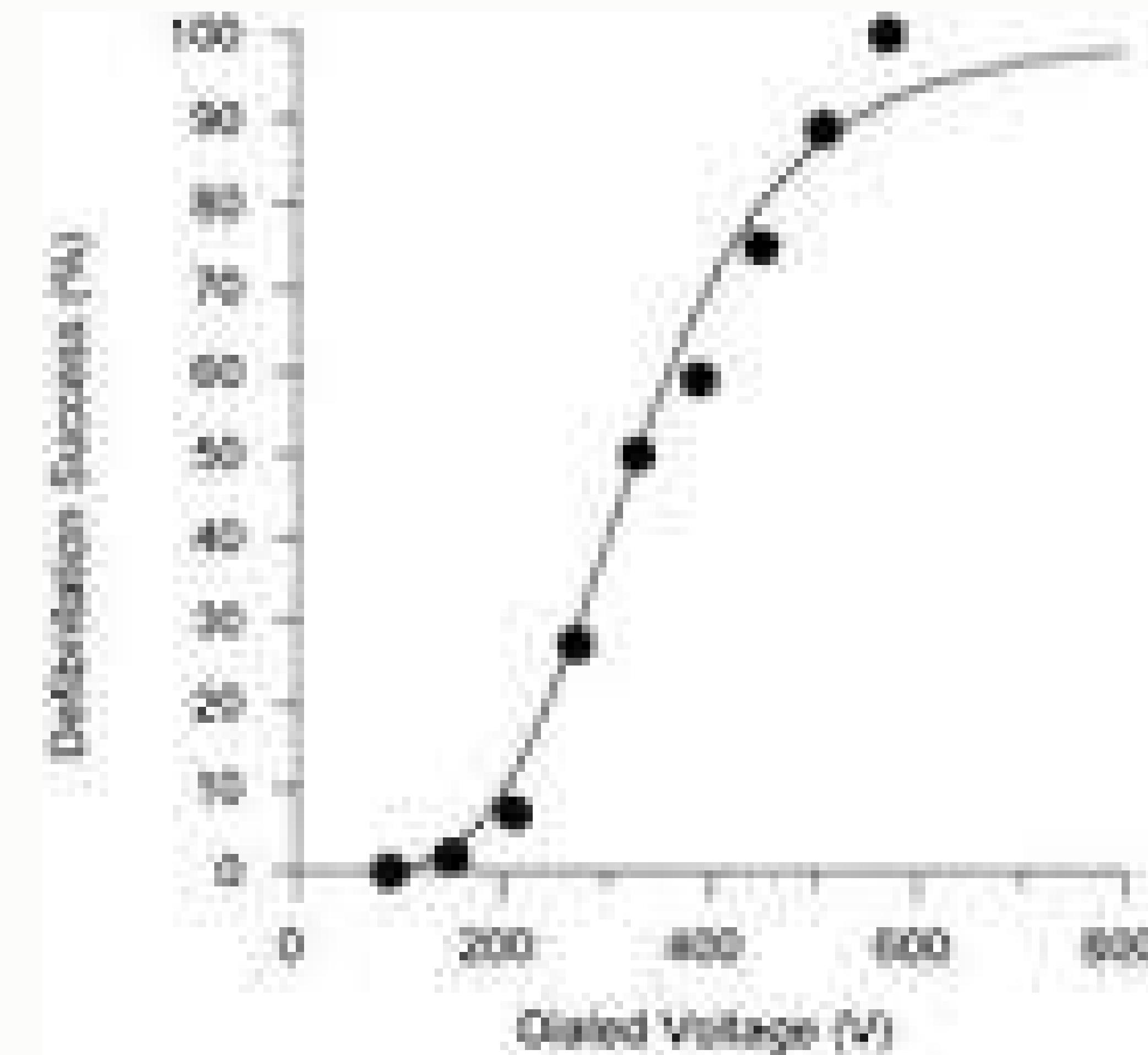
Super-threshold depolarization leads to **wave emission** if a short **rectangular electric field pulse** is applied.



Conventional defibrillation: termination with a single electrical pulse

Defibrillation success versus
shock voltage for 273 shocks
in 23 hearts

sigmoid dose-response curve
from: K.F. Kwaku and S.M. Dillon,
Circulation Research 79, 957–973 (1996)



Pulse timing matters

Strong temporal fluctuations in termination success rate

J. Steyer et al., to appear in: Frontiers in Network Physiology (2022)

Predictable ??

Terminating Cardiac Arrhythmias (Defibrillation) avoiding strong shocks

Sequences of weak pulses (LEAP)

Experiments:

S. Luther, F. Fenton et al., Nature 475 (2011)

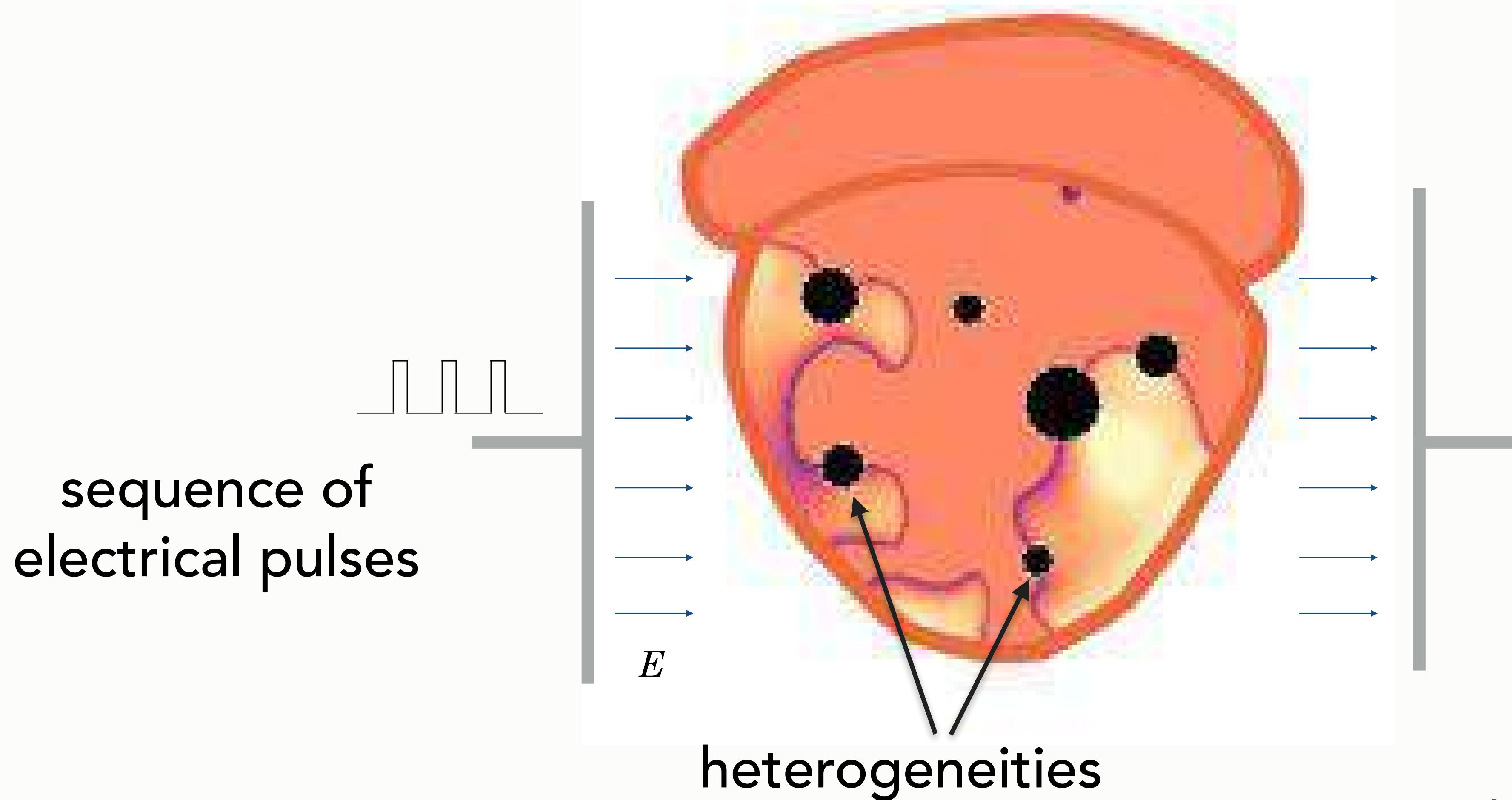
H. Janardhan et al., J. of the American College of Cardiology 63 (2014)

Simulations:

P. Buran et al., Chaos 27 (2017)

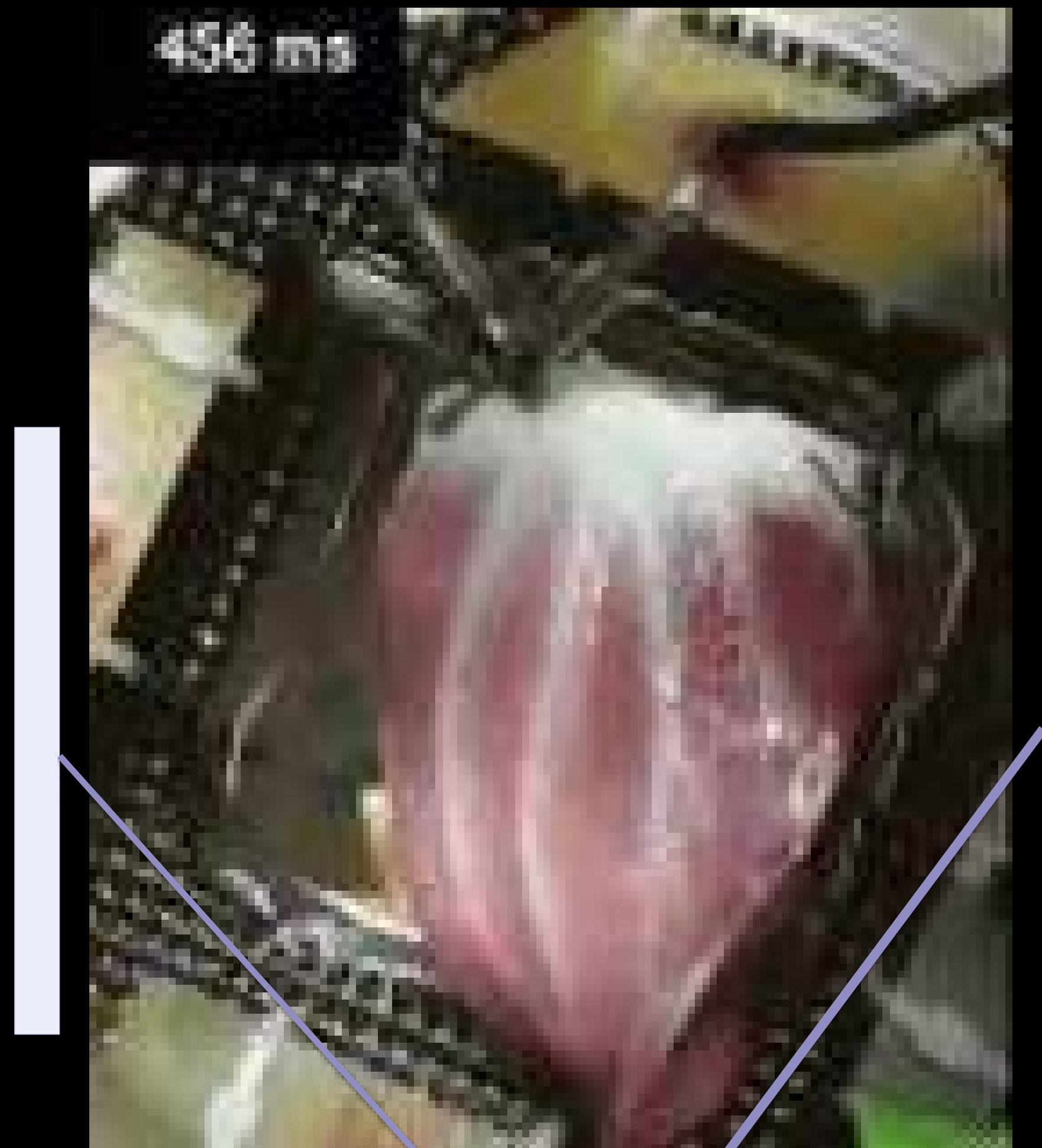
....

Recruiting Virtual Electrodes for Terminating Cardiac Arrhythmias



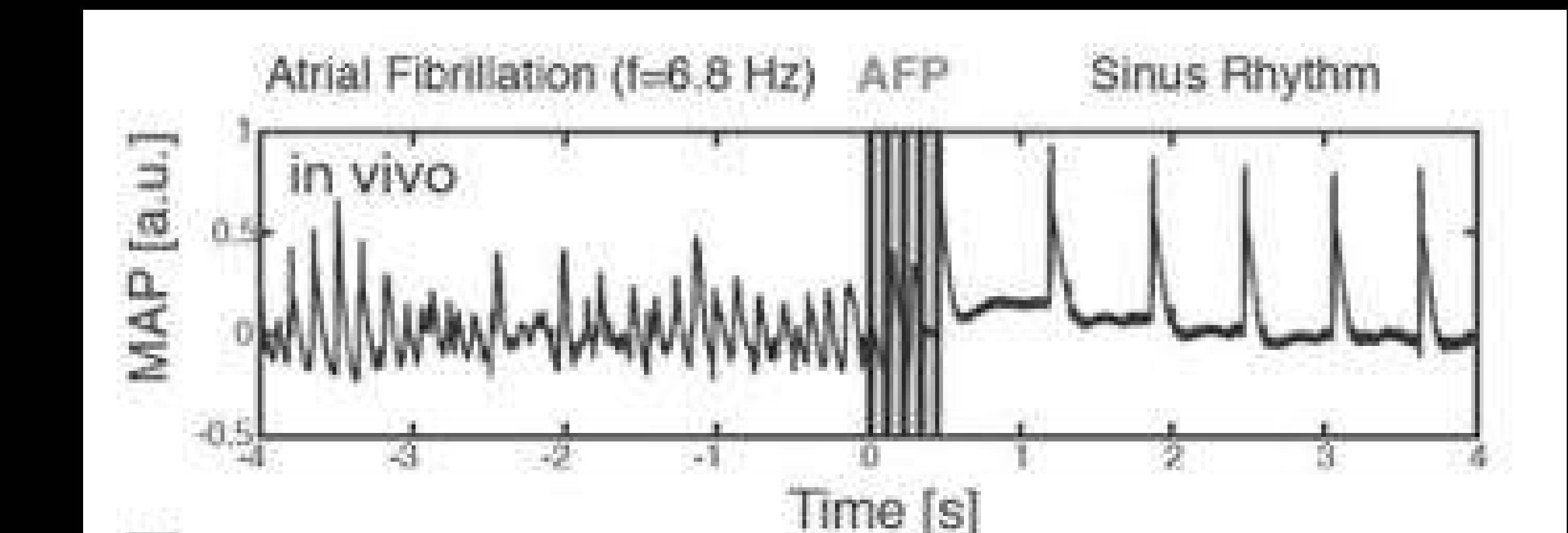
Animation: T. Lilienkamp

Low-Energy Anti-Fibrillation Pacing (LEAP)



Membrane Potential
20 mV -80

N = 5 low energy pulses
 $E = 1.4 \text{ V/cm}$
 $dt = 90 \text{ ms}$

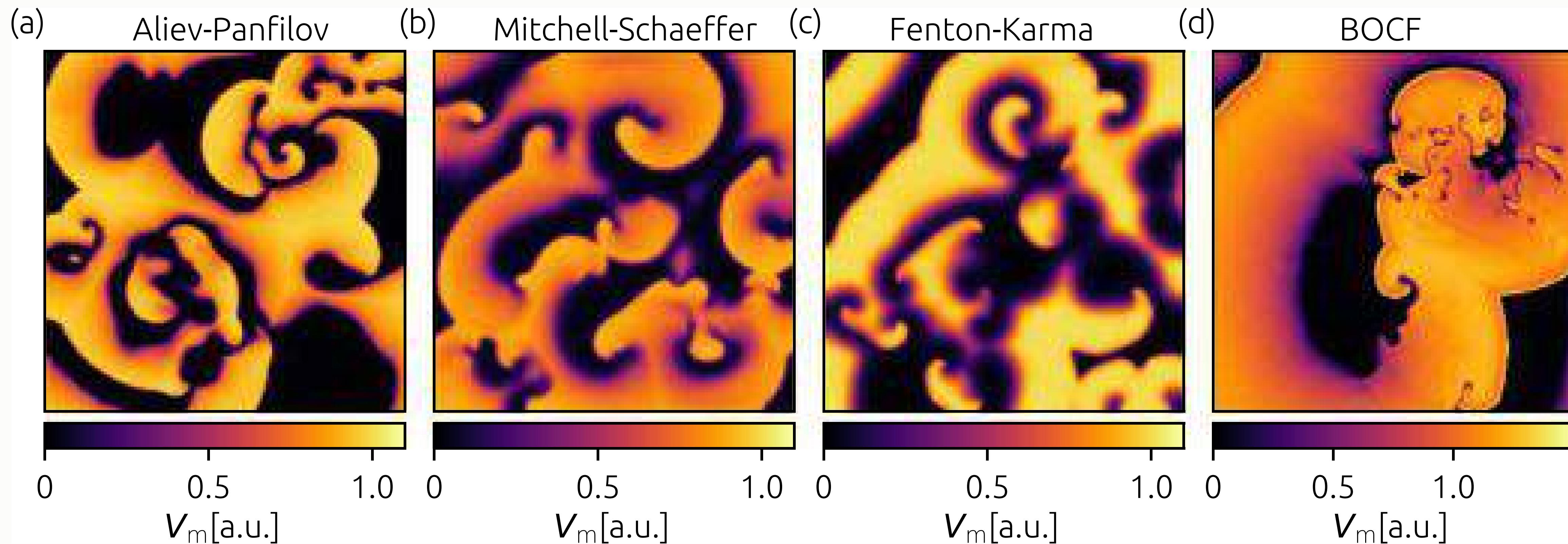


S. Luther et al., Nature 475, 235 (2011)

Impact of Pulse Sequences

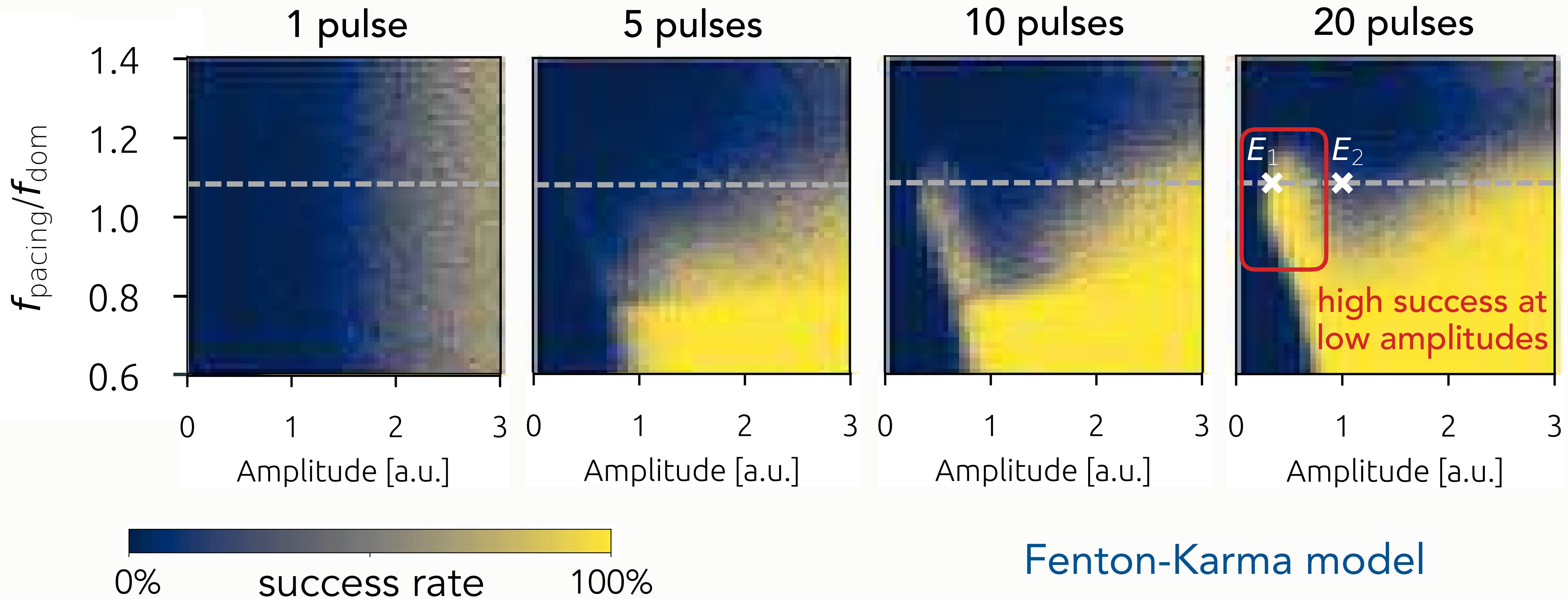
What does the dose-response curve look like for sequences of pulses?

Four model systems investigated



Termination Success Rate

Termination success rate vs. pacing amplitude and pacing frequency

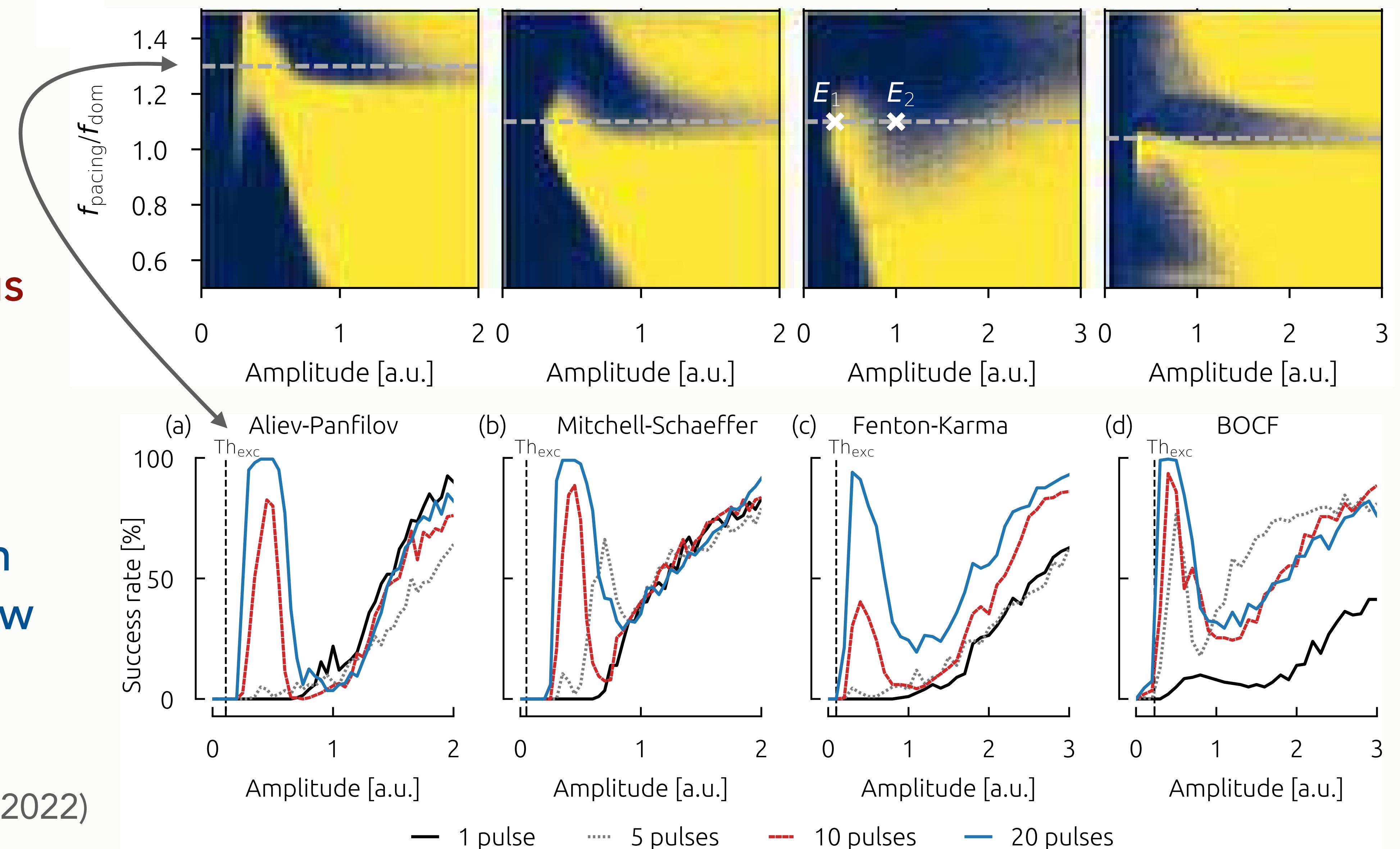


Non-monotonous Dose-Response Curve

Sequences
of pulses
result in

non-monotonous
dose-response
curves

with a peak of
high termination
probability at low
pacing energy



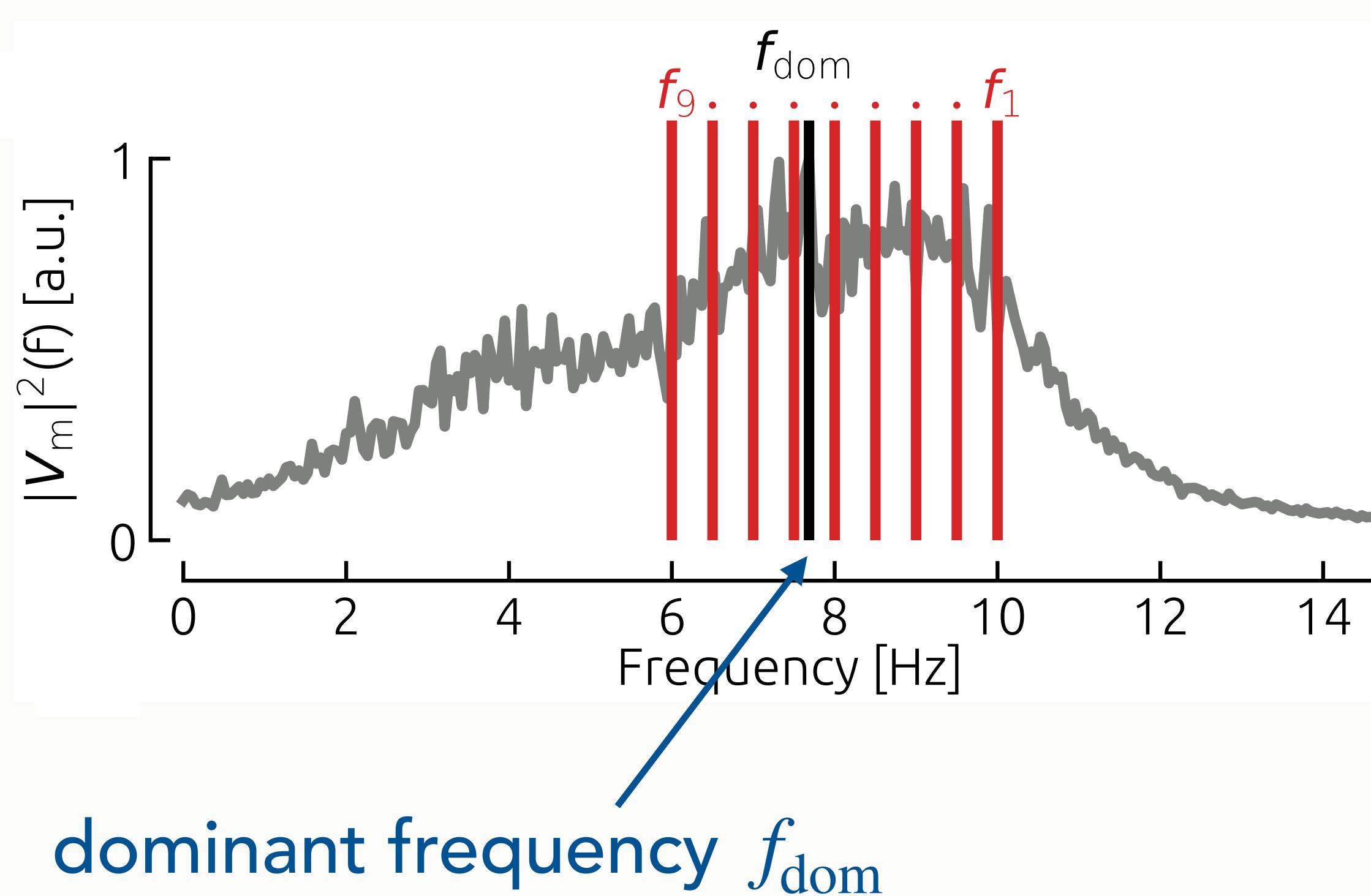
T. Lilienkamp et al.,
Scientific Reports 12 (2022)

Proper choice of pacing parameters is crucial

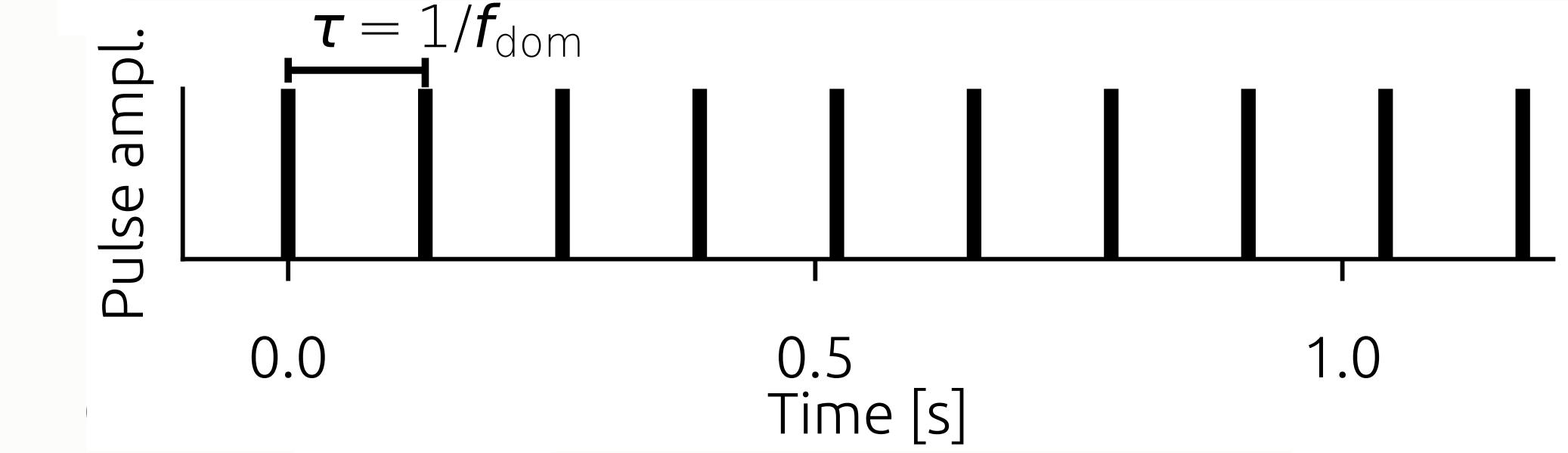
Non-equidistant Pulses

Use non-equidistant pulse sequences to cover a frequency range

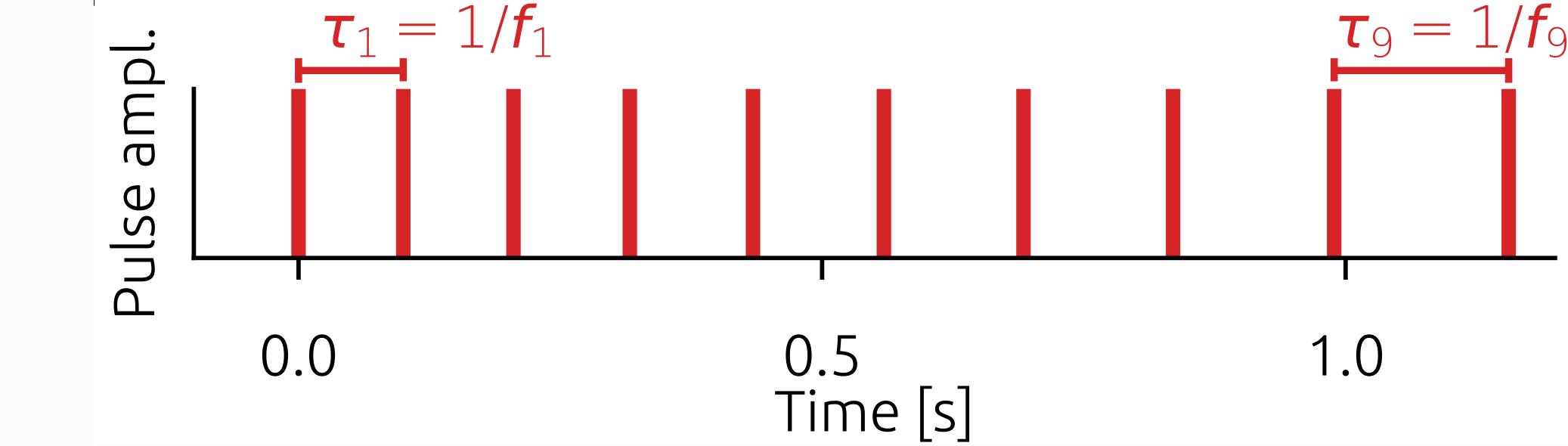
power spectrum (e.g., ECG)



equidistant pulses: $\tau = 1/f_{\text{dom}}$



non-equidistant pulses: $\tau_k = 1/f_k$

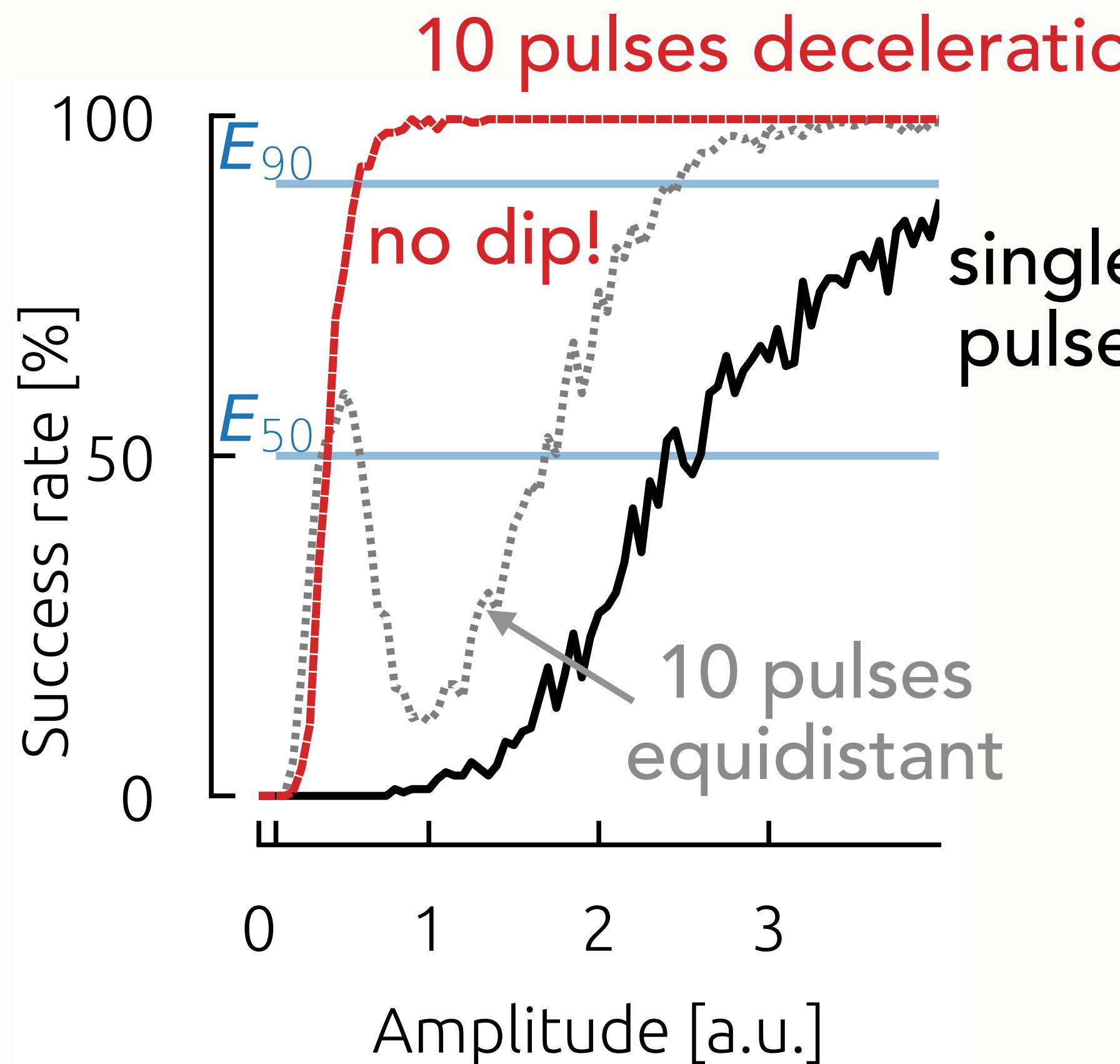


→ deceleration pacing

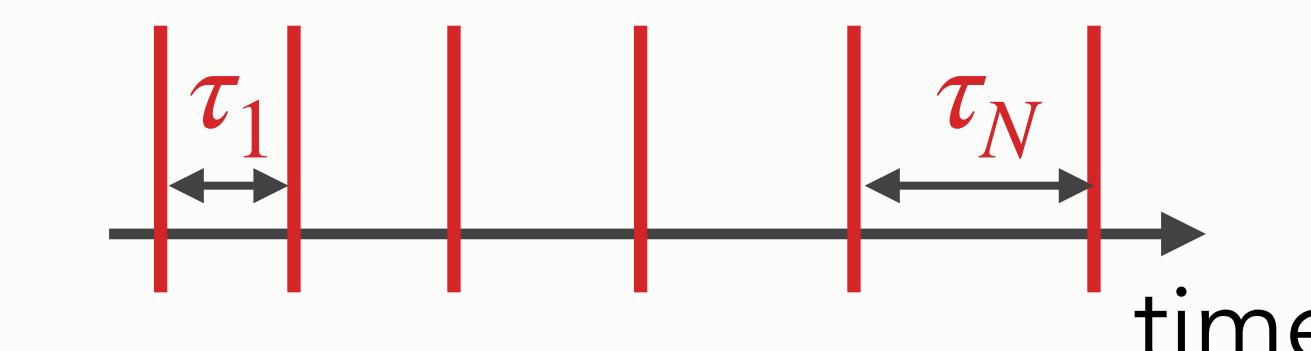
Linearly Increasing Inter-pulse Intervals

Dose-response curves

Fenton-Karma model

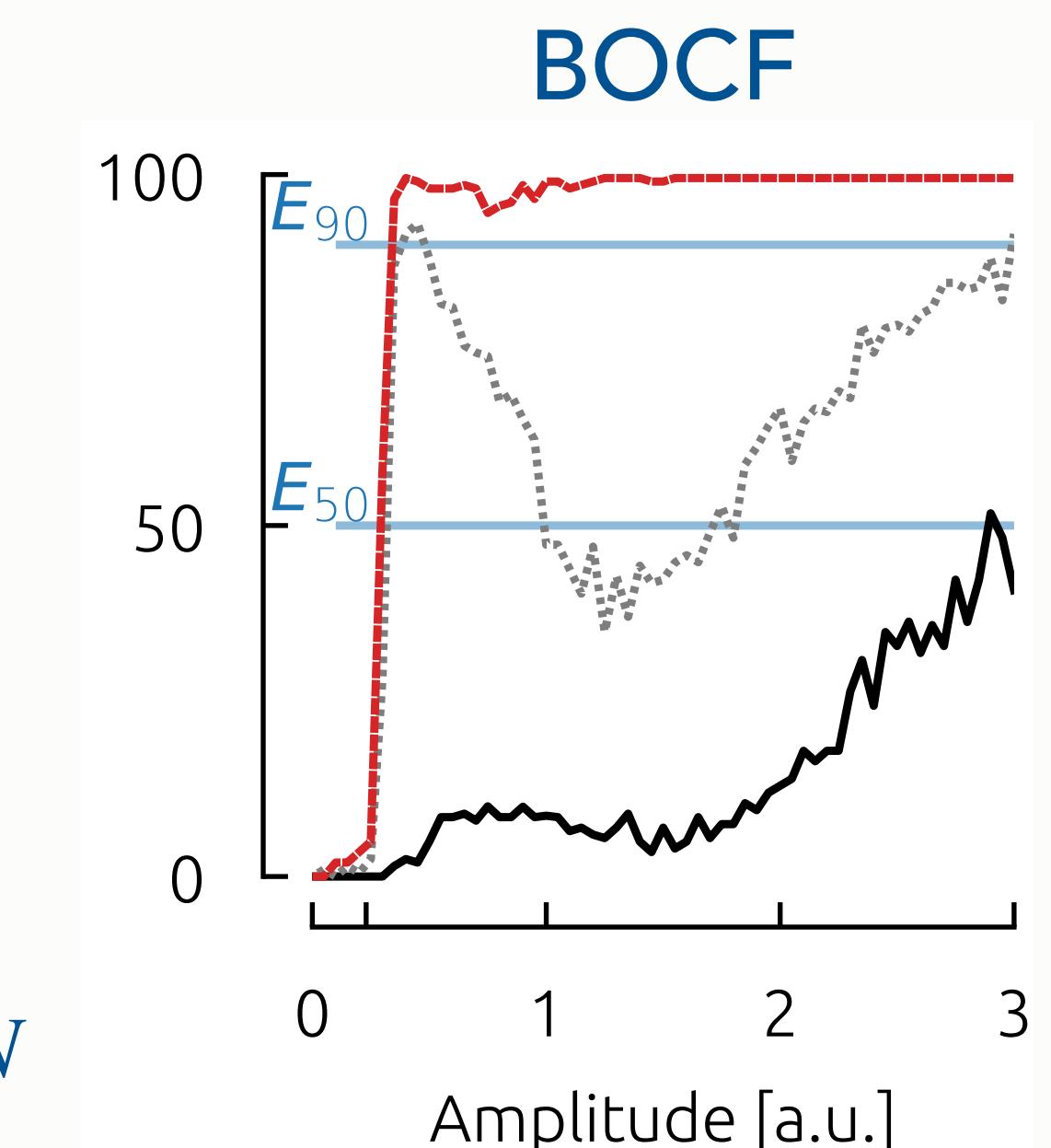


linear increase of
inter-pulse intervals



Choice of start τ_1 and end value τ_N is crucial and depends on model.

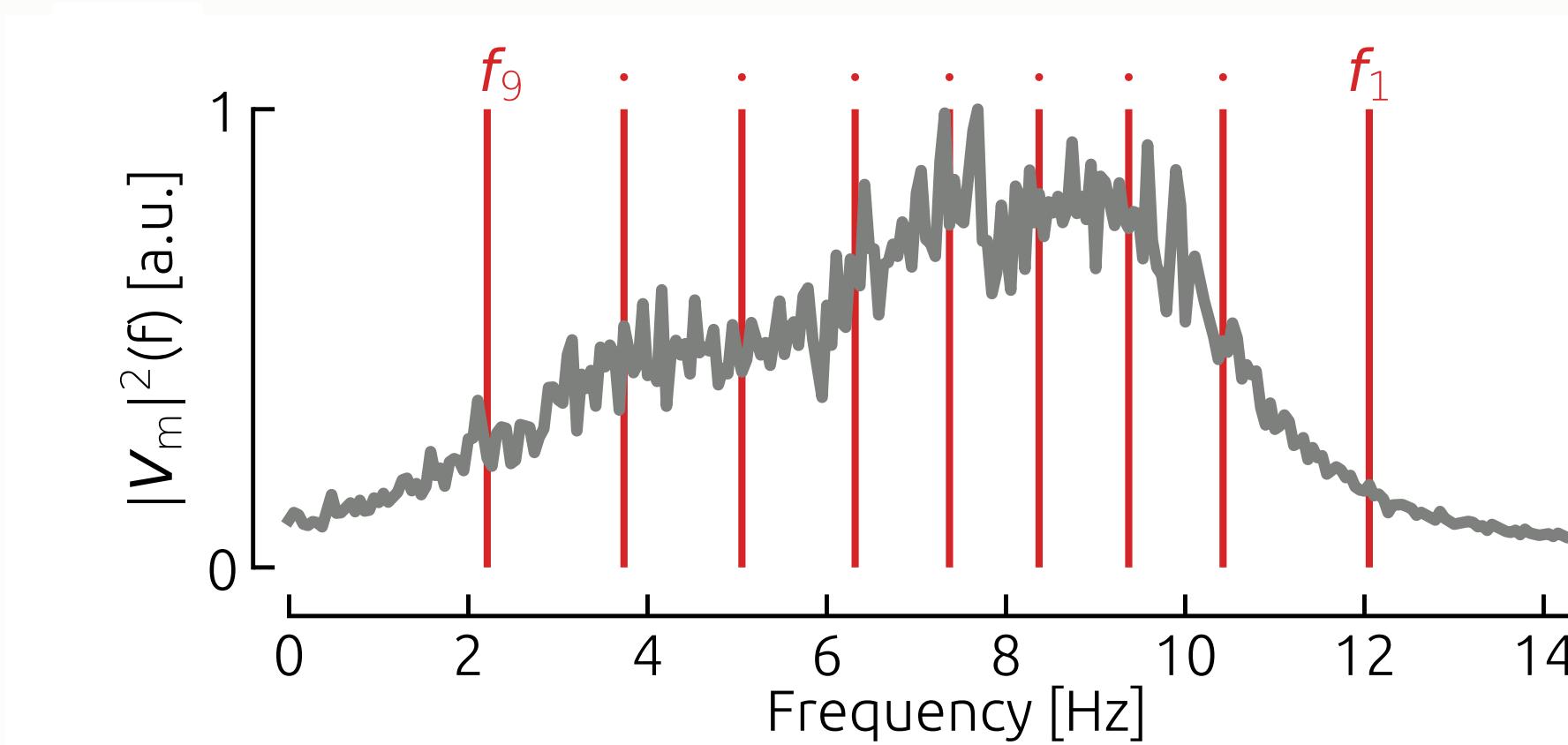
similar results for
other models



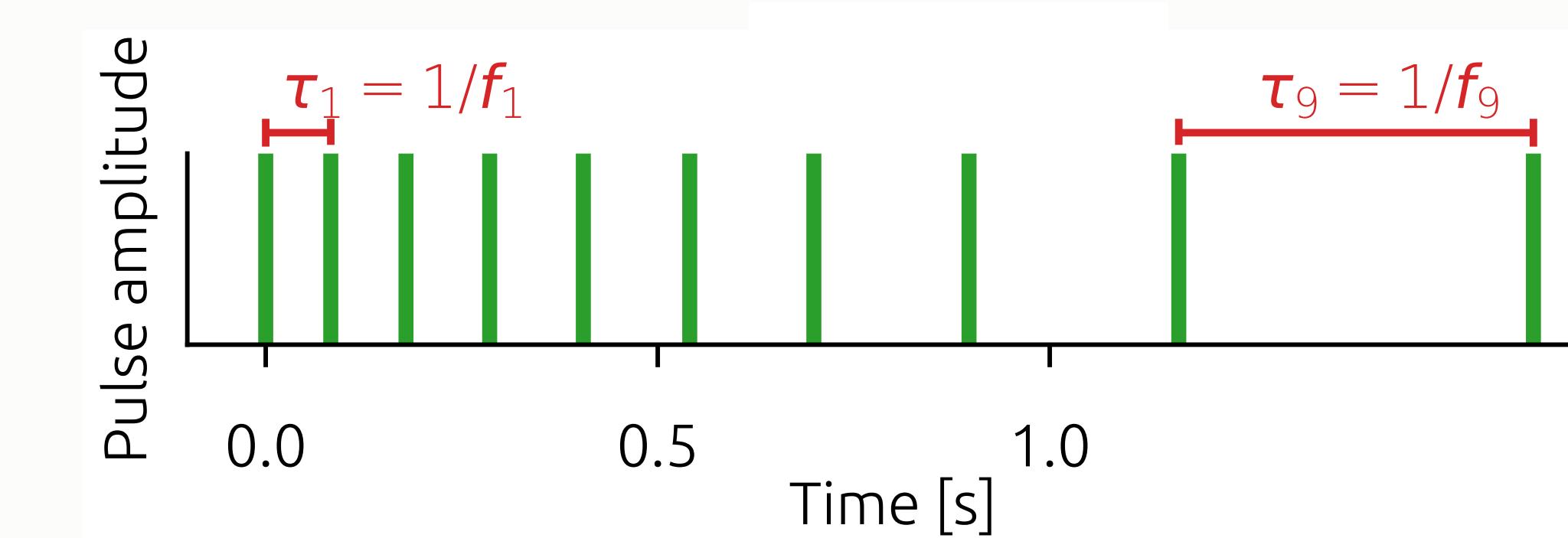
→ Need for a robust, model-independent protocol that is practical to use

Adaptive deceleration pacing (ADP)

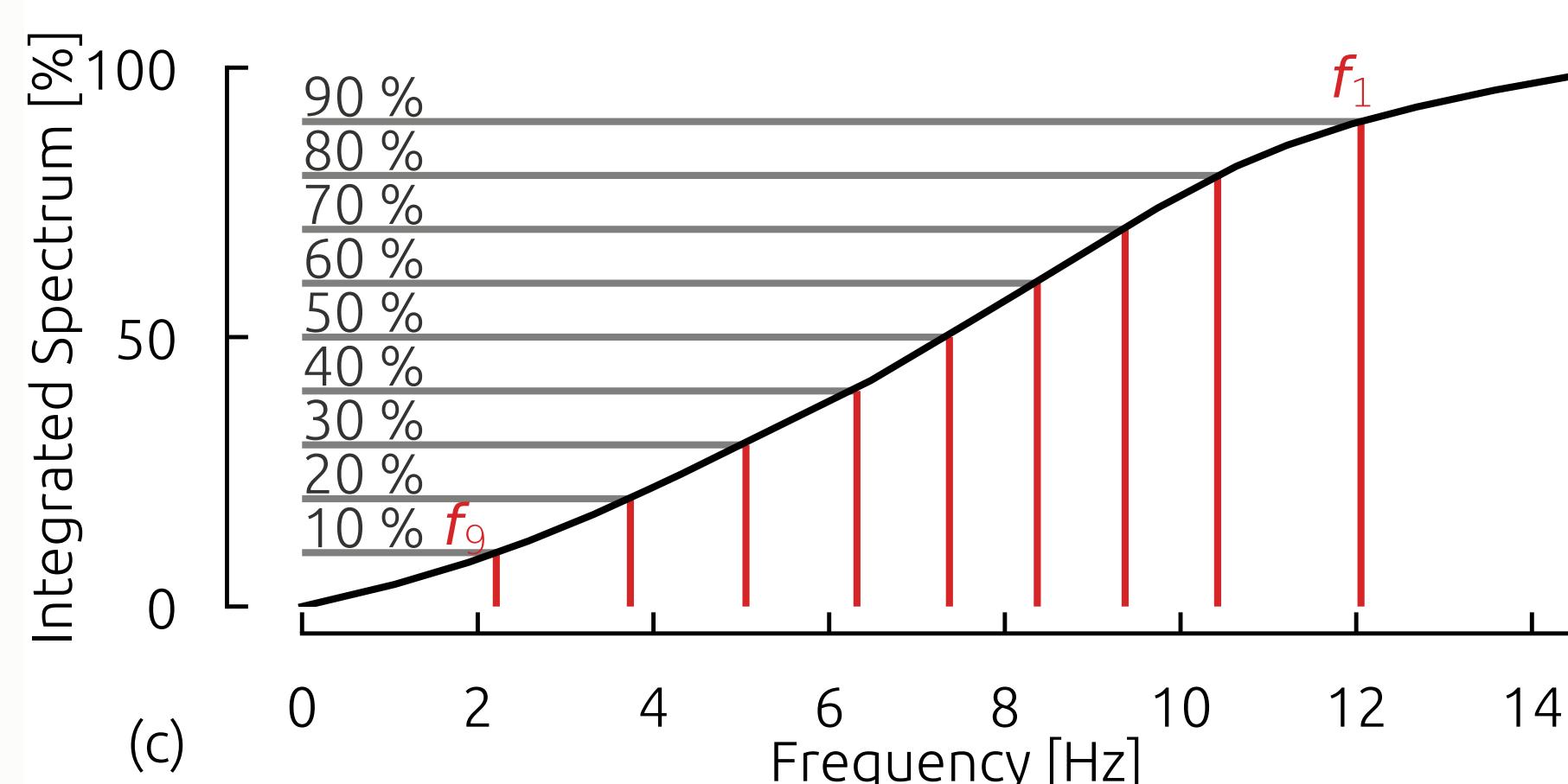
Fourier spectrum (e.g., ECG)



frequencies $f_k \rightarrow$ pulse intervals $\tau_k = 1/f_k$



Integral: equidistant levels $\rightarrow f_k$



- ADP pacing sequences are **highly adaptable** to the specific characteristics of the dynamics
- only **two free parameters**: cut-off frequency & no. of pulses
- **easy to implement** experimentally

Adaptive Deceleration Pacing

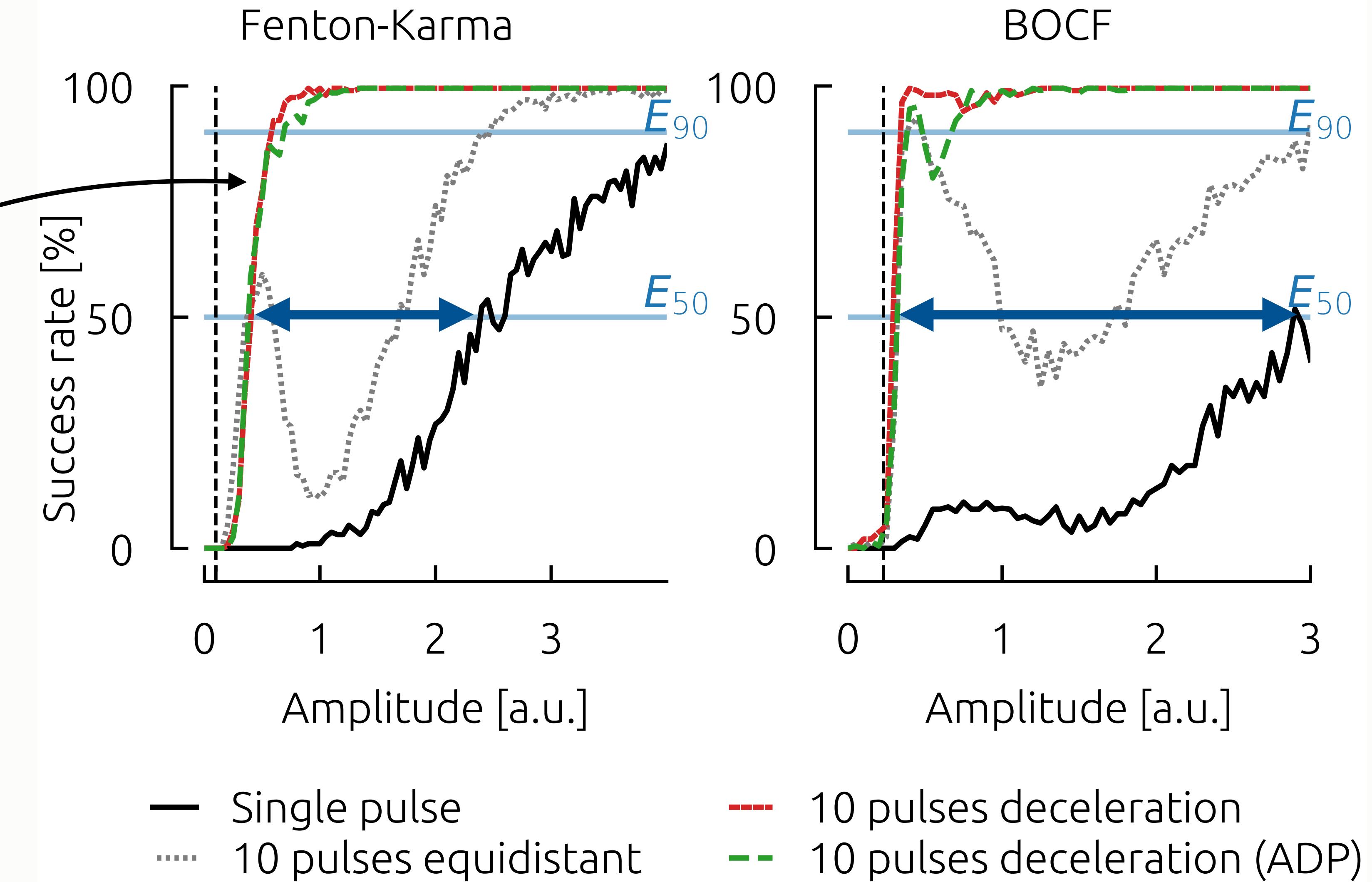
Adaptive deceleration pacing (ADP)

dose-response
curves

ADP almost as good
as linear deceleration
with carefully
selected start and
end frequencies

significant reduction of
required pulse amplitude

T. Lilienkamp et al., Chaos (2022)



Summary

- Ventricular fibrillation (VF) is a lethal state which requires immediate treatment: defibrillation using strong electrical shocks with side effects
- VF is closely connected to spiral wave chaos in excitable media
- data driven modelling is a promising approach to predict excitable cardiac dynamics and to reconstruct quantities that are difficult observe directly
- complex dynamics in excitable media can be governed by transient chaos with immediate consequence for its controllability
- pulse sequences of low energy may provide an alternative for defibrillation avoiding strong shocks with adverse side effects
- a novel and very promising approach employs adaptive deceleration pacing where pacing is slowed down in a systematic manner

Summary

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Thank you!



DZHK
DEUTSCHES ZENTRUM FÜR
HERZ-KREISLAUF-FORSCHUNG E.V.



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